

MULTIPLE LINEAR REGRESSION VIEWPOINTS
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MULTIPLE LINEAR REGRESSION VIEWPOINTS

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SOLUTIONS TO THE PROBLEM OF DISPROPORTIONALITY: A DISCUSSION OF THE MODELS*

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ABSTRACT

There are two major purposes of the paper. The first is to investigate the usefulness of a χ^2 technique in differentiating between varying degrees of disproportionality and their effects on a Type I error. The second purpose is to present and support the position that the major concern for any research model, whether disproportionate or not, is the research question and how well that question is reflected by the model. Three "exact solutions" for disproportional situations, the hierarchial, unadjusted main effects, and fitting constant methods, will also be discussed in terms of the research question that each reflects, and examples will be presented to demonstrate the most appropriate situation for using each solution.

This paper will deal with two main questions. The first will be to identify the effects of different degrees of disproportionality on the nominal level of Type I error and to test the assumption that a χ^2 test can be used to determine when disproportionality is severe enough that corrections are required.

^{*}This paper was presented at A.E.R.A., New York, NY, April, 1977.

The second part of this paper will deal with a discussion of some of the more prominent regression approaches ("exact" solutions) used to adjust for disproportionality.

The applied statistician and researcher is plagued with the problem of disproportional cell sizes in factorial experimental designs. This may occur because of mortality in the laboratory animals being used in the experiment; the required number of subjects not available; someone who had agreed to take part in the experiment fails to show up; or the data may represent the proportionality that exists in the "real world." (Disproportionality exists any time the expected values differ from the observed values. Obviously, one can have mild or severe disproportionality. The problem is to determine when the disproportionality is sufficiently severe to require adjustments. Therefore, this paper defines non-significant disproportionality on the bases of a χ^2 test where $\alpha=.25$ and significant disproportionality at $\alpha = .05$.) The effects on factorial designs by significantly disproportional versus non-significantly disproportional cell sizes, as determined by the chi-squared (χ^2) test, have not been studied, or at least reported. Such an investigation was attempted here.

Two studies were made, Study I and Study II. Each study contained four cases with 1,000 experiments per case, with the exception of the fourth case of Study II. In Study I, the main effects in each experiment were not necessarily significantly different. In Study II, the main effects in each experiment were made significantly different.

The following is a discussion of the paradigms used in each study.

The paradigm used in Study I was as follows:

- 1. Using a computer, 1,000 2 x 2 experiment tables were constructed for each of four cases--equal, proportional, non-significantly disproportional, and significantly disproportional cell sizes. Data points which were uniformly distributed and of equal variance were randomly generated in each of the cells [IBM, 1969].
- 2. Using computational formulas for sums of squares in the two-factor analysis of variance (ANOVA) with proportional cell frequencies, F-ratios and their corresponding probabilities were computed for each source of variability on each of the four thousand experiments.
- 3. The result of the analysis on the experiments containing equal frequencies was used as the measure of the actual probability level produced by this research procedure.
- 4. The probability levels produced by the analysis on the experiments containing significantly disproportional and non-significantly disproportional cell frequencies were compared to each other and to the actual probability level.

The paradigm used in Study II was the same as that for Study I with the exception that a value of five (5) was added to each of the data points of cells one and two so that the row factors were significantly different.

The procedures used in each of the two studies for obtaining the cell sizes, n_i (i=1,2,3,4), and to determine if the cell sizes were significantly and non-significantly disproportional were as follows:

Case I: Equal n's

A random number between ten and one hundred was generated and this became the size of each cell.

Case II: Proportional n's*

Since the cell sizes are proportional if $\frac{n_1}{n_2} = \frac{n_3}{n_4}$,

 n_1 , n_2 , n_3 were randomly generated and then n_4 was calculated from the equation $n_4 = \frac{n_2}{n_1}$,

where $10 \angle n_i \angle 100$, i = 1, 2, 3. See figure below for the labeling of the cells.

n ₁	n ₂
n ₃	n ₄

^{*}Determining n₄ in this manner most often resulted in actual values that ⁴ were non-integer numbers which the computer truncated to the integer value. Hence, n₄ differed from the true proportional value an amount x where $0 \le x < 1$.

Case III: Non-significant disproportional n's

Cell sizes n_1 , n_2 , and n_3 , were randomly generated, and then the proportional cell size n_4 was computed as in Case II. Then, so that the cell sizes were disproportional, a new n_4 , n'_4 , was calculated from the equation

$$n'_4 = n_4 + x + 1$$

where x is a randomly generated integer between one and ten. To determine if the cell sizes were non-significantly disproportional, a χ^2 test was made (p> α .25) where χ^2_{c} = 1.32--i.e., if $\chi^2_{a} \leq \chi^2_{c}$, the n's were judged to be non-significantly disproportional.

Case IV: Significant disproportional n's

Cell sizes n_1 , n_2 , n_3 , and n_4 , were randomly generated. To determine if the cells were significantly disproportional, a χ^2 test was made ($p \ge \alpha$.05) where $\chi^2_{\ c} = 3.841$ -i.e., if $\chi^2_{\ a} > \chi^2_{\ c}$, the n's were judged to be significantly disproportional.

The probability of a computed F-ratio was computed by using formulas 26.6.2, 26.6.10, 26.7.8, and 26.2.18 found in Abramowitz and Stegun [1967]. Algebraically, it can be shown that the above formulas combine so that the probabil-ity of a F-value for degrees of freedom in the numerator, v_1 , and degrees of freedom in the denominator, v_2 , is $P(F \mid v_1 = 1, v_2)^* = 1 - (1 + c_1 x + c_2 x^2 + c_3 x^3 + c_4 x^4)^{-4}$

^{*}P = .95 means that five times out of one hundred an F-value this large or larger would occur due to chance alone.

where $c_1 = .196854$, $c_2 = .115194$, $c_3 = .000344$, $c_4 = .019527$,

$$x = \frac{t (1 - \frac{1}{4v_2})}{\sqrt{1 + \frac{t^2}{2v_2}}}, \text{ and } t = \sqrt{F}.$$

TABLE I

PERCENTAGE OF SIGNIFICANT F-RATIOS FOR EACH OF THE FOUR CASES OF STUDY I

SOURCE	EQUAL n's	PROPORTIONAL n's	NON-SIGNIFICANTLY DISPROPORTIONAL n's	SIGNIFICANTLY DISPROPORTIONAL n's
Row Factor	5.60%	4.10%	4.60%	3.60%
Column Factor	4.60%	4.60%	4.40%	3.40%
Interaction	5.40%	5.40%	6.10%	806.9

TABLE II

PERCENTAGE OF SIGNIFICANT F-RATIOS FOR EACH OF THE FOUR CASES IN STUDY II

SOURCE	EQUAL n's	PROPORTIONAL n's	NON-SIGNIFICANTLY DISPROPORTIONAL n's	SIGNIFICANTLY DISPROPORTIONAL n's
Row Factor	100.00%	100.00%	100.00%	100.00%
Column Factor	6.408	3.90%	3.50%	* *
Interaction	4.80%	6,50%	11.10%	*

reject negative F-values. Hence, the process stayed within a loop and no results ** Interaction sums of squares were negative values. The program was written to were available.

The Monte Carlo data supports the position that mild cases of disproportionality versus severe cases of disproportionality, as operationally defined by the χ^2 , may be a useful approach in identifying the limits of when one cannot ignore effects of disproportional cells.

As one can see from Table I, when the null hypothesis is true, it appears that disproportionality does not present a problem. However, when the null hypotheses is not true and there is significant disproportionality, as measured by a χ^2 test (p \leq .05), the effects of the disproportionality cannot be ignored. In addition, the non-significant disproportionality case, (.25 < p < 1) as can be seen from Table II, has more frequently occurring significant interactions than occurred in the equal and proportional cases. Therefore, even in the non-significant case, the interaction may be more severely effected, and one should be sensitive to this possibility.

Obviously, this Monte Carlo study did not investigate the effects of both row and column being significant, row column and interaction being significant, or either row or column and interaction being significant. The reader should be aware that these situations may or may not produce different results than are presented in Tables I and II. However, the investigators feel that at this point, they have produced some supportive evidence for the potential usefulness for using a χ^2 to aid in decision making for determining when it is necessary to use corrections.

THREE REGRESSION SOLUTIONS FOR DISPROPORTIONALITY

when the researchers feel disproportionality is severe enough to be of concern, there are a variety of procedures that he can utilize to attempt to correct for the potential problems. However, before any corrections are applied, one should be sensitive to the underlying assumption that they are making about the population from which their data is drawn, and the investigator must also be very clear about the research question he is interested in asking.

If one had a research project in which the data and variables came from groups that already exist, such as age, intelligence, socio-economic status, etc., and if one was interested in generalizing and predicting back to the group from which the sample came, there is a good possibility that there would be a correlation that would not be spurious between such variables as I.Q. and socio-economic In other words, there may be significantly more above average socio-economic status people who have above average I.Q.'s than one would expect by chance. The data were forced to correspond to a balanced design in which there are an equal number of high and low I.Q. people for an equal number of high and low socio-economic status positions, the result of the study and the statistical analysis may allow one to say something that may only be true for that artificially forced relationship and one could not properly generalize to the population in which this

proportionality did not actually exist.

The other side of the coin is if the disproportionality in a research design is an artifact, (it really does not exist in the population) and the disproportionality of vectors is causing a spurious correlation between the variables, then one would have to adjust for this disproportionality and would have to decide which solution of disproportionality would best adjust the data so that it would better reflect the question(s) of interest and the true state of affairs.

To be able to begin to decide upon the correct solution, one has to

- a. know something about the theoretical and/or
 empirical relationship between the variables being studied;
- b. know some of the descriptive data about the population one wishes to generalize to in relation to the specific variables being studied;
- c. know the specific research question under investigation if one decides an adjustment for disproportionality is needed, then
- d. know the underlying assumptions and implications for different adjustment procedures, and
- e. know the consequences for using the selected adjustment procedure on the interpretation and generalization of the data.

Many researchers have dealt with items a - c but few have clarified the problems and implications related to

d and e on the above list. The following is a brief discussion of the underlying assumptions of some of the frequently used adjustments for disproportionality. It is hoped that this would aid researchers in being more sensitive to the questions they are really asking when writing models that reflect adjustment by different solutions for the problem of disproportionality.

There has been an exciting and thought provoking debate in the literature as to the most desirable (correct or accurate) procedure for correcting the problems of disproportionality. Most notably, Overall and Spiegel, 1969; Timm and Carlson, 1975; Overall, Spiegel, and Cohen, 1975; Werts and Linn, 1971; Rock, Werts, and Linn, 1976; and Applebaum and Cramer, 1973; have created the interest in the literature.

One basic way of organizing discussions on this topic is to categorize suggestions into two broad groups: approximate solutions or least sum of squares solutions. (This paper will discuss only the least sum of squares solutions.)

Three prominent least sum of squares solutions for disproportionality will be defined.

Solution I is the use of the general linear model to simultaneously adjust for the correlations between the main effects and the main effects with interaction. A symbolic example of this procedure is presented below for a two factorial design.

Model 1
$$Y_{kab} = \delta + b_1 \alpha_a + b_2 \beta_b + b_3 \alpha \beta_{ab} + \epsilon_{kab}$$

Model 2
$$Y_{kab} = \delta + b_4 \beta_b + b_5 \alpha \beta_{ab} + \epsilon_{kab}$$

Model 3
$$Y_{kab} = \delta + b_6 \alpha_a + b_7 \alpha_{ab} + \epsilon_{kab}$$

Model 4
$$Y_{kab} = \delta + b_8 \alpha_a + b_9 \beta_b + \epsilon_{kab}$$

Y_{kab} = is the score for subject k in row a and column b

 δ = is the grand \overline{X}

 α_a = is the effect for row "a"

 β_b = is the effect for column "b"

αβ_{ab} = is the interaction effect for the row "a" and column "b"

 ε_{kab} = is the error term for each subject

b, . . . b are partial regression coefficients

Adjustment for Solution #1

Adjustment for A main effects test Model 1 against Model 2

Adjustment for B main effects test Model 1 against Model 3

Adjustment for A*B effects test Model 1 against Model 4

(see also Figure I, P. 19)

Solution 2 adjusts each main effect in terms of the other main effects. The interaction was adjusted for by all main effects. (This is the same as in Solution 1). The following is a symbolic representation of this solution: (see also Figure II, P. 20)

Adjustment for Solution #2

Model 4
$$Y_{kab} = \delta + b_{10}\alpha_a + b_{11}\beta_b + \varepsilon_{kab}$$

Model 5
$$Y_{kab} = \delta + b_{12}\beta_b + \epsilon_{kab}$$

Model 6
$$Y_{kab} = \delta + b_{13}^{\alpha} \alpha_a + \varepsilon_{kab}$$

Adjustment for A main effects test Model 4 against Model 5

Adjustment for B main effects test Model 4 against Model 6

Adjustment for AB interaction effects test Model 4 against Model 1

Solution 3 assumes an apriori ordering of the importance of the variables under investigation. The apriori ordering decides which variables one will allow to account for as much variance as possible by themselves. The following is a symbolic representation of Solution 3, assuming the researcher considers the A main effects most important, B main effects second, and the interaction least important.

(Many researchers feel that it is unlikely that most investigators will be able to order the importance of their variable. However, we believe this judgment can be made by a competent researcher who is aware of the underlying constructs and theories he is dealing with) (see also Figure III, P. 21)

Admustment for Solution #3

Model 7
$$Y_{kab} = \delta + b_{14}^{\alpha} + \epsilon_{kab}$$

Model 8
$$Y_{kab} = \delta + \epsilon_{kab}$$

Model 9
$$Y_{kab} = \delta + b_{15}^{\alpha} + b_{16}^{\beta} + \varepsilon_{kab}$$

Adjustment for A main effects test Model 7 against Model 8

Adjustment for B main effects test Model 9 against Model 7

Adjustment for AB interaction test Model 1 against Model 9

Marks (1974) presents a mathematical proof that one has to have to A main effects and B main effects in the full and restricted models to test for AB interaction. It seems that this is true when dealing with traditional analysis of variance and catagorical variables. That is, the A main effects and B main effects must be fitted first before interaction can be tested. However, this does not seem to be necessarily true when dealing with continuous variables. To the best of our knowledge, this has never been investigated.

Most researchers, specifically the highly mathematically oriented statisticians, tend to evaluate the accuracy of the above three least square solutions for disproportionality in terms of some arbitrary mathematical matrices often based upon unfounded underlying assumptions. A more logical method for deciding upon which solution is most appropriate in a specific case would be to be aware of the underlying assumptions for each of the structural models of each solution and assumptions about the relationship between the variables being studied.

In a 2 x 2 orthogonal design, the correlation between the A main effect, B main effect, and the AB interaction is zero. Therefore, the effects of the A main effect in predicting the criterion can be totally attributed to the A main effect; similarly for the B main effect and the AB interaction. However, when the design is non orthogonal (disproportional n's) correlations between the A main effects, B main effects, and AB interaction are likely. Therefore, the effect of A in predicting the criterion is not necessarily independent of the B main effect and AB interaction.

Each of the three least square solutions make different assumptions about the meaningfulness and "usefullness" of the correlations between the A main effect, B main effect, and AB interaction.

Solution 1, for example, when testing the A main effect, assumes the correlation between A and B and the AB interaction is of an accidental nature, and therefore should not be considered (Rock, et al., 1976). This solution is most likely to be prefered when one can assume that the missing subjects producing disproportionality were random. If one is unable to make this assumption, then it would be inappropriate to use Solution 1, (which may be the case most frequently).

Solution 2 assumes that there is no correlation between the A and B main effects in the population. Therefore, the correlation between A and B in the sample is a function of disproportionality and not representative of the population. Solution 2 then attempts to adjust for this correlation.

However, Solution 2 assumes that the correlations between the main effects and the interaction, which results from the disproportionality, are not spurious and are characteristic of the population. Therefore, it does not attempt to adjust for this correlation.

If one cannot assume that the correlations between the A and B main effects, due to disproportionality, are due to chance, than Solution 2 would be an inappropriate correction.

Solution 3 requires an apriori ordering of the importance of each variable. Let us assume that the apriori ordering are: A main effects, B main effects, AB interaction, respectively.

When testing for the A main effects, Solution 3 assumes that the correlation between the A main effects, B main effects, and A main effects with the AB interaction is representative of the relationship between these variables in the population and therefore relevant to the research question of interest. That is to say, the relationship between these variables are not artifacts of disproportionality.

However, when testing for B main effects, Solution 3 assumes that the correlation between the A main effect and B main effect is not relevant and is therefore an artifact of unequal N's. It also assumes that the correlation between the A main effects and the interaction, and the B main effects and the interaction is not due to just a chance relationship caused by disproportionality.

The key to the most appropriate selection of these three solutions is not as much a statistical concern (mathematical) but rather a comprehensive understanding of the data so that one can more accurately speculate on which correlations between the variables are likely to be meaningful or not meaningful.

FIGURE I

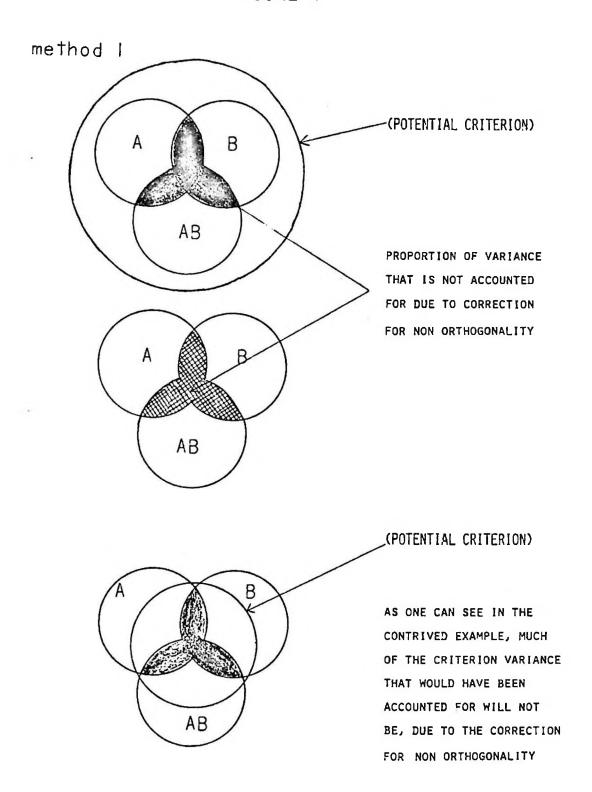


FIGURE II

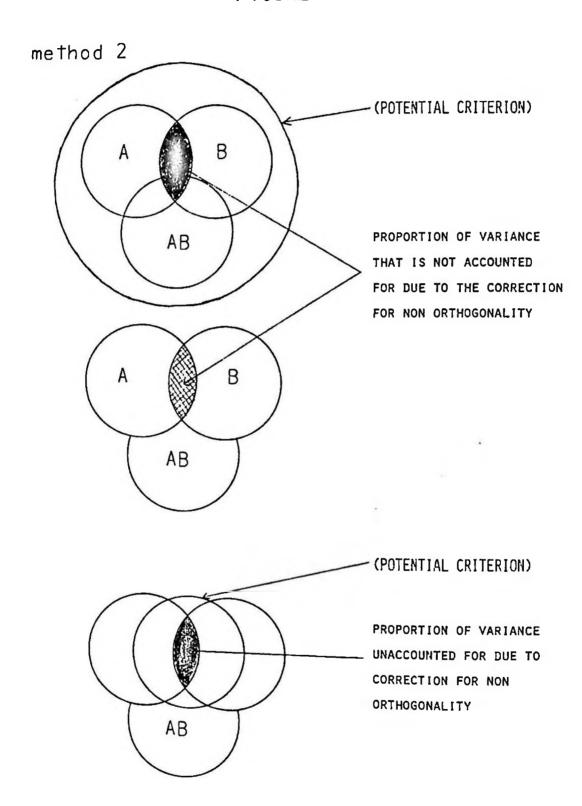
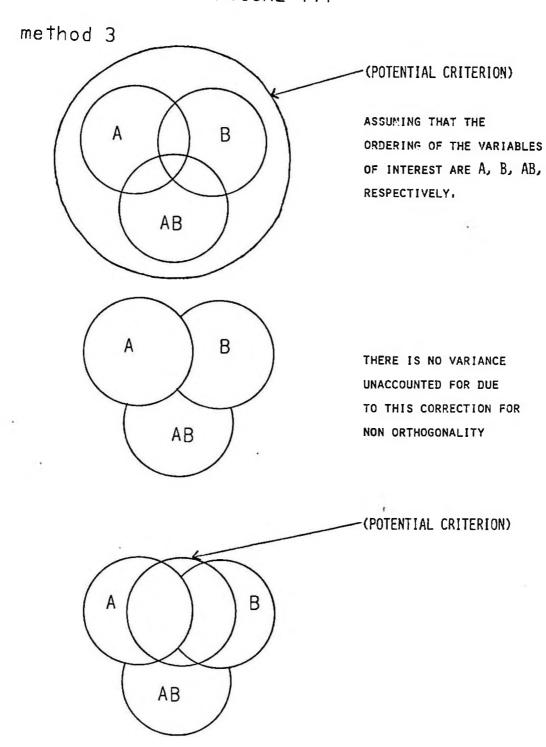


FIGURE III



SOME ADDITIONAL CONSIDERATIONS

Since the three solutions previously discussed are only defined for use with fixed designs, it is initially important to define the basic statistical models of fixed randomized and mixed effects. The fixed effect model is a model in which all the variables have levels which are fixed. That is, the levels of a variable that is to be investigated are determined prior to the investigation. These categorical (high, medium low, etc.,) determinations set the limits to which the investigator can generalize his results.

Randomized effect is a design in which the researcher randomly selects the level of variable that is to be investigated from an infinitely large number of possible levels. This allows the researcher to generalize his results to the entire range of the variable being investigated (that is to the extent that the levels were truly randomly selected and are representative).

The mixed effect model has at least one fixed effect variable and one random effect variable.

Most research conducted is on fixed effect models. This model has a great deal research behind it which indicated that the model is very robust. This means, it is little effected by violations of its assumptions of normality, homogeneity, etc. However, this robustness is not true of the randomized effects model. This model is very sensitive to violations of normality and homogeneity of

variance. Most interestingly, in terms of the purpose of this paper, is that the assumptions of equal N's is absolutely essential for deriving correct error terms for randomized effect designs. 1

Assuming that one is dealing only with a fixed effect design, one alternative is to consider the correlation between the variables, due to the disproportionality as accurately existing in the population one wishes to generalize to. Then, the researcher may choose not to correct for the disproportionality. The problems that arise with this, is that one cannot attribute the variance accounted for to a particular variable. (This is the dilema of much ex post facto research.)

In conclusion, as can be seen from the discussion in Part II of this paper, it appears obvious that it would be inappropriate to attempt to decide on a correction for disproportionality by using Monte Carlo Studies. Since the appropriateness of a solution depends upon the correlations as one can assume to exist between the variables in the population, and this can change from population to population or with varing theoretical positions, it is much more relevant to try to understand these relationships and base your solution on this understanding than to base

¹ To our knowledge, there has been no research on methods for correcting unequal N's in randomized designs.

your decision on the outcome of generated data in which the relationships may be totally unrelated to the relationships in the population of interest.

A highly detailed discussion of different solutions to the hypothesis being tested can be found in Searle (1971). There exists problems that go beyond the scope of this paper such as what occurs when interactions are included in the model and one or more cells equal zero; Searle (1971), Marks (197), and Williams (1977), deal with the problems of full versus non-full ranked matrices; Williams (1977) indicates potentially different effects on solutions due to the effects of different coding procedures. All of these questions are of interest.

Owever, once again the key is to understand your research questions and the assumptions about the relationships that exist among your variables as reflected by your models.

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APPENDIX

WJIVI

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10/38/49
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C ONLLO OSAVECZ-NEWMAN HYPOTHESIS - FOLIAL N'S CASE
C MOCIFIED FROM ON100 3-2-76 WD WHEATON ROW PACTOR NOT
                                           NECESCARILY SIGNIFICANT
C DEFINITION - 2X2 CONTINGENCY TABLE
C CELL (1.1) FOU CELL (1)
C CELL(1,2) FOU CELL(2)
C CELL(2,1) EQU CELL(3)
  CELL(2,2) FOU CELL(4)
      SEAL#4 P(4), SUM(4), SUMS(4), F(3), PF(3), PRCT(6)
      INTEGER*4 N(4), NSIG(3), DATE(4)
     FOULVALETICE (SUM(1).SUM1). (SUM(2).SUM2). (SUM(3).SUM3).
     1(SUM(41, SUM4), (M(1), N1), (N(2), N2), (N(3), N3), (N(4), N4),
     2(F(1),FR),(F(2),FC),(F(3),FRC)
 200 FURMAT('1', 35X, 'UN110 GRAVECZ & NEWMAN EQUAL N''S CASE
     1,4A2,T123,'PAGE',13//
            CELL SIZE RATIOS
                                                 CELL POPULATION SIZE
     21
                                             (1,1) (1,2) (2,1) (2,2)
                  (1,2) (2,1) (2,2)
                COL TABLE ROW COL TABLE 1/
      FORMAT(F8.5,3F9.5,1X,4I7,1X,3E12.4,1X,3F9.5)
 201
 202 FORMAT( ! 10N110 ORAVECZ & NEWMAN EQUAL N''S CASE . 1,4A2///
     111X. PERCENT OF CASES'/
     210X, 18('-')/
                   N'DIZ-NCM
     312X, 'STG
     410X, 1----
     5' ROW '.2F11.2//
6' COL ',2F11.2//
     7' TIBLE' 2F11.2/// TOTAL CASES RUN = 1.16)
C GET CURRENT DATE
      CALL TDATE(DATE)
C CONSTANT NEEDED LATER D1=2,/9,=0,222222
      D1=0.222222
C PROBABILITY EXPANSION CONSTANTS
      CC1=0.196854
      SC2=0.115194
      CC3=0.000344
      CC4=0.019527
C NUMBER OF CASES TO RUN
  NUMBER OF NON-SIGNIFICANT CASES - ROW, COL & TABLE
      NS 16(1)=0
      NSIG(2)=0
      MSTG(3)=0
C PAGE & LINE CHTS
      LINE=100
   .IPAGE=1
T LOOP OUTE ALL CASES
      DO 306 K=1.NC
C GENERATE CELL SIZE (.GT. 10)
 YI = XI UCE
      CALL RANDULIX. LY . PPI
      NN=PP*100°
      IT (NN.LT. 10) GC TO 300
C SET ALL CELLS FOUND & SET CELL PERRAPILITIES TO DIE
```

1. INE = 6

...307

1046==1046"+1

LINE=LINE+1

NETT (6, 201) P.N. F. P.

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C GNILO ORAVECZ-NEWMAN HYPOTHESIS - EQUAL N'S CASE
C MORIFIED FROM ON100 . 3-2-76 MD WHEATON . ROW FACTOR SIGNIFICANT C DEFINITION - 2X2 CONTINGENCY TABLE
   CELL(1.1) .EQU CELL(1)
   CELL(1+2) EQU CFLL(2)
 C
   CELL(2,1) EQU CELL(3)
 C
   CELL(2,2) EQU CELL(4)
      REAL*4 P(4), SUM(4), SUMS(4), F(3), PF(3), PRCT(6)
      INTEGER*4 N(4), NSIG(3), DATE(2)
      EQUIVALENCE (SUM(1), SUM1), (SUM(2), SUM2), (SUM(3), SUM3),
    1(SUM(4), SUM4 L.(N(1), N1), (N(2), N2), (N(3), N3), (N(4), N4).
     2(F(1),FR),(F(2),FC),(F(3),FRC)
  200 FORMAT('1', 35X, 'ONII) ORAVECZ & NEWMAN EQUAL N''S CASE
 1,4A2,T123, 'PAGE', 13//
2' CELL SIZE RATIOS
3 F VALUES
                                            CELL POPULATION SIZE
                                          PROBABILITIES!/
  201 FORMAT(F8.5, 3F9.5, 1X, 417, 1X, 3E12.4, 1X, 3F9.5)
 202 FORMAT('ICN110' DRAVECZ & NEWMAN EQUAL N''S CASE ', 2A4///
     111X, 'PERCENT OF CASES'/
  210X,18('-')/
312X,'SIG NON-SIG'/
410X,'-----//
     5' ROW ',2F11.2//
6' COL ',2F11.2//
     7' TABLE', 2F11.2///' TOTAL CASES RUN =',16)
C GET CURRENT DATE

CALL TDATE(1,DATE)
C CONSTANT NEEDED LATER D1=2./9.=0.222222.
      D1=0.222222
 C PROBABILITY EXPANSION CONSTANTS
      CC1=0.196854
    CC2=0.115194 ·
    CC3=0.000344
CC4=0.019527
C NUMBER OF CASES TO RUN
      NC=1000
 C NUMBER OF NON-SIGNIFICANT CASES - ROW, COL & TABLE
   NSIG(1)=0
      NSIG(2)=0
NSIG(3)=0
C PAGE & LINE CHTS
      LINE=100
      IPAGE=1
IY=9
C LOOP OVER ALL CASES
DO 306 K=1,NC
C GENERATE CELL SIZE (.GT. 10)
 300 IX=IY
      CALL RANDU(IX, IY, PP)
     IF(NN.LT. 10) GO TO 300
   NN=PP *100.
 C SET ALL CELLS EQUAL & SET CELL PROBABILITIES TO ONE
_____ DO 301 1=1,4
```

```
N(I) = NN
               P(1)=0.25
               CONTINUE
     301
               NSUM=4*NN
 C GENERATE MEMBERS OF EACH CELL & CELL SUM
               TSUMS=0.0
DO 303 I=1,4
     310
SUM(I)=0.0
                                                       the second part and the se
                 SUMS(I)=0.0
               L=N( { }
 DO 304 J=1,L
               IX=IY
               CALL RANDU(IX, IY, A)
         IF(I.LE.2) A=A+5
               SUM(I)=SUM(I)+A
               SUMS(I)=SUMS(I)+A*A
304 CONTINUE
               TSUMS=TSUMS+SUMS(I)
     303 CONTINUE
   C CALC ROW, COL, & TABLE SUMS
           CALC ROW, COL, & TABLE SUMS SO ROW FACTOR SIGNIF
               R1S=SUM1+SUM2
               R2S=SUM3+SUM4
               C1S=SUM1+SUM3
               C2S=SUM2+SUM4
               TABSUM=R1S+R2S
   C CALC ROW, COL, $ TABLE SUMS SQUARED
               TSS=TABSUM*TABSUM/FLOAT(NSUM)
               SSR=R1S*R1S/(N1+N2)+R2S*R2S/(N3+N4)-TSS
               SSC=C1S*C15/(N1+N3)+C2S*C2S/(N2+N4)-TSS
               SST=TSUMS-TSS
             SSCELL=SUM1*SUM1/N1+SUM2*SUM2/N2+SUM3*SUM3/N3+SUM4*SUM4/N4-TSS
               SSRC=SSCELL-SSR-SSC
               SSERR=SST-SSR-SSC-SSRC
C CALC F VALUES FOR ROWS, COLS, & TABLE
               DF=NSUM-4
               SERRM=SSERR/DF
               FR=SSR/SERRM
               FRC=SSRC/SERRM
C IF F(1) IS NEGATIVE DROP CASE FROM CONSIDERATION
                IF(FR.LT.0.0) GD TO 310
                IF(FC.LT.0.0) GO TO 310
                IF(FRC.LT.0.0) GO TO 310
    C CALC PROBABILITIES FOR ROWS, COLS & TABLE
                C2=D1/DF
On 305 I=1,3
                X1=SQRT(F(I))*(10-0-25/DF)/SQRT(10+005*F(I)/DF)
               X2=1.0+X1*(CC1+X1*(CC2+X1*(CC3+X1*CC4)))
                X3=X2*X2*X2*X2
                PF(I)=10-10/X3
    C CNT NON-SIGNIFICANT CASES - RCH, COL & TABLE
               IF(PF(I).LE.0.95) NSIG(I)=NSIG(I)+1
305 CONTINUE
    C PRINT CASE PARAMETERS
               IF(LINE.LE.56) GC TO 307
                LINE=6
           IPAGE=IPAGE+1
```

```
MAIN
LEVEL 21
                                         DATE = 76162
                                                                09/12/36
     WRITE(6,201)P,N,F,PF
     LINE=LINE+1
306
     CONTINUE
C CALC' SIGNIFICANT CASES, PERCENTAGES, & PRINT SUMMARY
     DO 308 L=1,6,2
     M = L/2 + 1
     LSIG=NSIG(M)
     MSIG=NC-LSIG
     PRCT(L)=FLOAT(MSIG)*100/ANC
     PRCT(L+1)=FLDAT(LSIG)*100/ANC
308
     CONTINUE
     WRITE (6,202) DATE, PRCT, NC
     STOP
     END
```

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C ONIDO DEAVICZ-	ALCHMAIL HY	OTHESIS	- PPOPOK	TTOGĀLĪCĀ	<u>s: </u>		
	7.6 WIN WHITE	עווו ג		tetor No	T Canada Caa	CT	
C DEFINITION - 5	VO CONTINO	SENCY TAB	LE PECE	SARILY SI	LPMI PI CATA	٠,	
C DEFINITION -	CELL(1)	32110					
C_CELL(1.1) EQU	CELL (2)		7.0				
C CFLI. (11,2) Full	, 6511121						
C CELL(2,1) FOL	, (50, (4)				and the same of th		
C CFL1 (2,2) FQ1), \$IIM(4),	TIME LAN.	(3) .PF(3	PRCT(6)			
F: 4[×4 P (4	1) , SIM(4) ;	104314111 121 DATE	4)				
INTEGER*4	N(4),NSIG	CHULL 15	11M121 SIII	181121.159	31 - SUM3		
LOUIVALING	E (SUMILL)	POUTTING		21. N21. (NIAL NA		
1(0)(4),5	IM4),(:)(1)	rrii), twice	21 +14 21 +1 +1	(3) (10) (11	· · · · · · · · · · · · · · · · · · ·	*	
2(=(1),=0)	, (£(2), =C)	, (= (3) , = =	CT C NEW	MAN DOORD	DTIONAL	CELL	C1756 .
200 FORMATULE	<u>.35X, UNI</u>	O OF ANT	CZ & NEW	AN PROPO	RITUNAL	1.611	21/27
1,442,7123	, 'PAGE', 13	//		651	I BODIII	TTON	
2'	CELL SIZE				L POPULA		
3	F VAL	UES			<u>PROBABII</u>		2'/
41							
5							'/
6' (1,1)	(1.2)		(2,2)		(1.2)		
7 ROW	CDI	_	TABLE	ROW	CUI	-	TABLE'/
8'				~~			-
9							
201 FORMAT(F8.	5,3F9.5,1	K,417,1X,	3F12.4,1	(+3F9.5)			
202 FORMAT(11)	MIDO OCINE	PECZ & NE	WMAN PROF	PORTIONAL	CFLL ST	ZF\$	1,442///
111X, 'PERCE	INT OF CASE	S1/ /					
210X, 18('-'						T.	
312X, 'SIG		161/	1.5				
410X, '							
5' ROW 1,2			·······				
61 COL 1,2	2F11.2//						
7' TABLE!		TOTAL CA	SEC DUN -	-1 7/1			
C GET CURRENT DA	T =		1353 VOA 3				
CALL TDATE							
C CONSTANT NEED	ED LATED I	11-2 (0 -					
71=0.22221	22	11-60/70=	Jo 221722				
C PROBUCILITY ()		TAICTANTE					
CC1=0.1968	154 154	71919112					
CC 2=0.115				·			
003=0.070							
<u> </u>							
C NUMBER OF CAS	ES TO DUAL						
NC=1000	TO FOR						
C NUMPER OF NON.	-SIGNICIO	UT CASE					
C NUMPER OF NON-	STONI - ICE	VI CASES	- ROW, COL	& TABLE			
MSTG(2)=9							
NS 16(3)=0							
C PAGE & LINE C	NTC						
LTM=100	412			-1			
1 <u>P</u> ^CF=1.							
Iv=9	•••		• • • • • • • • •				And the state of
C LOCK GVER ALL	CACCE						
20 306 K=	1 45 5						
C GENERATE CELL	1 Th.						
300 IX= 14	21.5 ('C	To 101					
[/II DAMO	11110						42
VINI-DD#130	ULIX.IV.PP	1					
TEINE IN							
C CALC COLL CO	וטו פח דף	300					
STALC COLL SIZ	.2						
120 4=0		-		222			

FEAGI	71	MAIN	DATE = 7609	2 10/48/45
	01 301 Lal	.3		
302	I y = I Y			
-	CALL RANDU			
		o) GO.TO 302		
	M(I)=NM IE[MM*F1*I	0) 60.10 102		
	, ,	REL		
301	CONTINUE			
	N4=N2*N3/N	1		
CIF	N4 IS_LESS_	THAN 5 DROP CASE	0	
) GO TO 300		
	NSUM=NSUM+	194	•	
	00 309 [=1	• 4		7
	4M=N(I)			
	P(1) = AN/SU	4N		
309	CONTINUE			
-		RS OF SECH CELL BUCELL	SUM	
310	TSUMS=0.0			·
	00 303 I=1			
	SUM(I)=0.0 SUMS(I)=0			
+	L=((I)			
	00 304 J=1	, L		
	IX=IY		4,	
	CALL RANDU			
	SUM(I)=SUM			
304	SUMS(I)=SU CONTINUE	MS(1)+A*A	1	
704	TSUMS=TSUM	S+SUMS(1)		
303	CONTINUE	3.30/13(1)		(4)
		TABLE SUMS		
	RIS=SUM1+S			
	R2S=SUM3+S			
	C1S=SUM1+S			•
•	C2S=SUM2+S			
C CALC	RIN COL .	TABLE SUMS SQUARED		
o one.	TSS=TARSHM	*TABSUM/FLOAT(NSUM)		
	SSR=R1S*R1	S/(N1+N2)+R2S*R2S/(N3+1	V4)-TSS	
	SSC=C1S*C1	S/(N1+N3)+C2S*C2S/(N2+)	N4)-TSS	
	SST=TSUMS-	TSS		T. C.
	SSCELL=SUM	1 *SUM1/N1+SUM2*SUM2/N2	<u>+SUM3*SUM3/N3+SUM</u>	4" SUM4/ N4-155
	SSRC=SSCEL	L-SSR-SSC		
C CAL	SSCRR=SSI-	SSR-SSC-SSRC EDR POWS, COLS, E TABLE		
	DF=NSIJM-4	EUR SHWY, DILDE JABLE		
	SERRM=SSER	R/DF		
	E3=552/SEP	SM		
		RM Committee of the com		
C 15	FRC=SSPC/S	EPR.M		
-X-1-	TELED INFO	ATTVE DROP CASE FROM CO	DNSIDERATION	
	THIR TIND	•0) GO TO 310		
	IF (FRC-IT)	•01 GD TO 310 0•01 GU TO 310		
C CAL	PROBABILI	TIES FOR ROWS, COLS & TA	ABLE	
			7 V % L	
	CO_335_1=1	1.3		
	x1=20s1(5(I))*(1J.25/DE)/SORT(Lo+O,5*F(1)/DF)	

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```
C ON100 ORAVECZ-NEWMAN HYPOTHESIS - PROPORTIONAL CASE
      C WRITTEN 2-11-76 WD WHEATON
                                                                                                                                 ROWFACTOR SIGNIFICANT
      C DEFINITION - 2X2 CONTINGENCY TABLE
            CELL(1,1) EQU CELL(1)
               CELL(1,2) EQU CELL(2)
               CELL(2,1) EQU CELL(3)
      C
               CELL(2,2) EQU CELL(4)
. . C
                         REAL*4 P(4), SUM(4), SUMS(4), F(3), PF(3), PRCT(6)
                         INTEGER*4 N(4), NSIG(3), DATE(2)
                         EQUIVALENCE (SUM(1),SUM1),(SUM(2),SUM2),(SUM(3),SUM3),
                      1(SUM(4), SUM4), (N(1), N1), (N(2), N2), (N(3), N3), (N(4), N4),
                      2(F(1),FR),(F(2),FC),(F(3),FRC)
      200 FORMAT('1',35X,'ON100 ORAVECZ & NEWMAN PROPORTIONAL CELL SIZES
                      1,4A2,T123, PAGE , 13//
                                                             CELL SIZE RATIOS
                      21
                                                                                                                                                                   CELL POPULATION SIZE
                                                               F VALUES
                                                                                                                                                                             PROBABILITIES'/
                                  (1,1) (1,2) (2,1)
                      61
                                                                                                                        (2,2) (1,1) (1,2)
                                                                                                                                                                                                                       TABLE'/
                                  ROW
                                                                                                                         TABLE
                                                                                                                                                         ROW
                                                                                                                                                                                 · COL
                     8 1
                                                                                                                                                           ____
                        FORMAT(F8.5,3F9.5,1X,4I7,1X,3E12.4,1X,3F9.5)
         202 FORMAT( 1GN100 ORAVECZ & NEWMAN PROPORTIONAL CELL SIZES 1, 244///
                     111X, PERCENT OF CASES'/
                      210X,18('-')/
                     312X, 'SIG
                                                                       NON-SIG'/
                     410X, '---
                     5' ROW ',2F11.2//
                     6' COL
                                                ',2F11.2//
                     7' TABLE', 2F11.2///' TOTAL CASES RUN =',16)
      C GET CURRENT DATE
                         CALL TDATE(1,DATE)
     C CONSTANT NEEDED LATER D1=2./9.=0.222222
                         D1=0.222222
      C PROBABILITY EXPANSION CONSTANTS
                        CC1=0.196854
                         CC2=0.115194
                         CC3=0.000344
                         CC4=0.019527
                                                                                                                                The second state of the control of t
     C NUMBER OF CASES TO RUN
                         NC=1000
    C NUMBER OF NON-SIGNIFICANT CASES - ROW, COL & TABLE
                        NSIG(1)=0
                        NSIG(2)=0
                         NSIG(3)=0
    C PAGE & LINE CHTS
                        LINE=100
                         IPAGE=1
                         1Y=9
     C LOOP OVER ALL CASES
                         CO 306 K=1.NC
C GENERATE CELL SIZE (.GT. 10)
                        CALL RANDU(IX, IY, PP)
                        NN=PP*100.
                         IF(NN.LT.10) GO TO 300
  C CALC CELL SIZES
                                                                              and the second s
                        NSUM=0
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	. 21	MAIN		•	1/43/
	00 301 I=1.3				
202					
302	IX=IY CALL RANDU(IX:	-IY-A)			
	CALL KANDOLIA				
	NN=A+100. IF(NN.LT.10)	SO TO 302			
	ILINATION (00 ,0 202			
	N(I)=NN				
	NSUM=NSUM+NN				ī
301	CONTINUE				1.
	N4=N2*N3/N1	N 4 DDAD CASE			
CIF	N4 IS LESS THAT	O TO 300			
	IF(N4.LT.6) G	0 10 300			
	NSUM=NSUM+N4			_	
	SUMN=NSUM			19	4.
	DO 309 I=1,4				
	AN=N(I)				
+	P(I)=AN/SUMN				
309	CONTINUE		Class		
C GEN	RERATE MEMBERS	OF EACH CELL & CELL	SUM		
310	TSUMS=0.0			<u> </u>	1 6
	DO 303 I=1,4				
5	SUM(1)=0.0	A 41 W. 1	and the same of the same of		
	SUMS(I)=0.0	***	- W	, E	
	L=N(I)				. 4
	DD 304 J=1.L				
	IX=IY	<u></u>			
	CALL RANDULIX	,IY,A)	and the second second		2.90
	IF(I.LE.2) A=			The property	4
	SUM(I)=SUM(I)			· · · · · · · · · · · · · · · · · · ·	
	SUMS(I)=SUMS(3 . 1	
20/			The state of the s		
304	CONTINUE				
304		UMS(I)	,		
304	TSUMS=TSUMS+S	UMS(I)	· · · · · · · · · · · · · · · · · · ·		
303	TSUMS=TSUMS+S			· Jaguara	
303 C CAI	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA	BLE SUMS	CTOD SIGNIE	Ly. Yagawa	
303 C CAI	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, &	BLE SUMS TABLE SUMS SO ROW FA	ACTOR SIGNIF	a temperature	
303 C CAI	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2	BLE SUMS TABLE SUMS SO ROW FA	CTOR SIGNIF		
303 C CAI	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4	BLE SUMS TABLE SUMS SO ROW FA	CTOR SIGNIF		
303 C CAI	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3	BLE SUMS TABLE SUMS SO ROW FA			
303 C CAI	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4	BLE SUMS TABLE SUMS SO ROW FA	ACTOR SIGNIF		
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2	BLE SUMS TABLE SUMS SO ROW FA			
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA	BLE SUMS TABLE SUMS SO ROW FA			
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM)			
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N	14.1-12C		
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM+TA SSR=R1S+R1S/(SSC=C1S+C1S/(BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N) N1+N3)+C2S*C2S/(N2+N)	14.1-12C		
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N) N1+N3)+C2S*C2S/(N2+N)	(4)-TSS (4)-TSS		
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N	(4)-TSS (4)-TSS		TSS
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSRC=SSCELL-S	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N SUM1/N1+SUM2*SUM2/N2+SSR-SSC	(4)-TSS (4)-TSS		TSS
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N SUM1/N1+SUM2*SUM2/N24 SR-SSC	(4)-TSS (4)-TSS		TSS
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N SUM1/N1+SUM2*SUM2/N24 SR-SSC	(4)-TSS (4)-TSS		TSS
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSRC=SSCELL-S LC F VALUES FOR DF=NSUM-4	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N UM1/N1+SUM2*SUM2/N24 SR-SSC C-SSC-SSRC ROWS,COLS,& TABLE	(4)-TSS (4)-TSS		TSS .
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N UM1/N1+SUM2*SUM2/N24 SR-SSC C-SSC-SSRC ROWS,COLS,& TABLE	(4)-TSS (4)-TSS		TSS
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D FR=SSR/SERRM	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N UM1/N1+SUM2*SUM2/N24 SR-SSC C-SSC-SSRC ROWS,COLS,& TABLE	(4)-TSS (4)-TSS		TSS
303 C CAI C	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D FR=SSR/SERRM FC=SSC/SERRM	BLE SUMS TABLE SUMS SO ROW FA BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N UM1/N1+SUM2*SUM2/N2+N SR-SSC ROWS,COLS,& TABLE OF	N4)-TSS N4)-TSS -SUM3*SUM3/N3+SUM4-	*SUM4/N4-1	TSS
C CA	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D FR=SSR/SERRM FC=SSR/SERRM FRC=SSR/SERRM	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N UM1/N1+SUM2*SUM2/N24 SR-SSC C-SSC-SSRC ROWS,COLS,& TABLE OF	14)-TSS 14)-TSS -SUM3*SUM3/N3+SUM4	*SUM4/N4-1	TSS
C CA	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & RIS=SUM1+SUM2 R2S=SUM2+SUM4 C1S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D FR=SSR/SERRM FRC=SSR/SERRM	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N3+N N1+N3)+C2S*C2S/(N2+N SR-SSC C-SSC-SSRC ROWS,COLS,& TABLE OF	14)-TSS 14)-TSS -SUM3*SUM3/N3+SUM4	*SUM4/N4-1	TSS
C CA	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & RIS=SUM1+SUM2 R2S=SUM2+SUM4 C1S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSCELL=SUM1*S SSC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D FR=SSR/SERRM FC=SSC/SERRM FRC=SSRC/SERRM FRC=SSRC/SERRM FRC=SSRC/SERRM FRC=SSRC/SERRM FRC=SSRC/SERRM FRC=SSRC/SERRM	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N2+N N1+N3)+C2S*C2S/(N2+N SR-SSC C-SSC-SSRC ROWS,COLS,& TABLE OF (WE DROP CASE FRCM CO	14)-TSS 14)-TSS -SUM3*SUM3/N3+SUM4	*SUM4/N4-1	TSS
C CA	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & RIS=SUM1+SUM2 R2S=SUM2+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D FR=SSR/SERRM FRC=SSR/SERRM	BLE SUMS TABLE SUMS SO ROW FA SS. BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N2+N N1+N3)+C2S*C2S/(N2+N SR-SSC RSSC-SSRC ROWS,COLS,& TABLE OF CM (VE DROP CASE FRCM CO) GO TO 310	N4)-TSS N4)-TSS SUM3*SUM3/N3+SUM4 ONSIDERATION	*SUM4/N4-1	TSS
C CA	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D FR=SSR/SERRM FC=SSR/SERRM FC=SSR/SERRM FRC=SSR/SERRM FRC=SSR/SERRM	BLE SUMS TABLE SUMS SO ROW FA S BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N2+N N1+N3)+C2S*C2S/(N2+N UM1/N1+SUM2*SUM2/N24 SR-SSC C-SSC-SSRC ROWS,COLS,& TABLE OF (VE DROP CASE FRCM CO D GO TO 310 CO TO 310	N4)-TSS N4)-TSS SUM3*SUM3/N3+SUM4	*SUM4/N4-1	TSS .
C CA	TSUMS=TSUMS+S CONTINUE LC ROW, COL, & TA CALC ROW, COL, & R1S=SUM1+SUM2 R2S=SUM3+SUM4 C1S=SUM1+SUM3 C2S=SUM2+SUM4 TABSUM=R1S+R2 LC ROW, COL, \$ TA TSS=TABSUM*TA SSR=R1S*R1S/(SSC=C1S*C1S/(SST=TSUMS-TSS SSCELL=SUM1*S SSCELL=SUM1*S SSRC=SSCELL-S SSERR=SST-SSR LC F VALUES FOR DF=NSUM-4 SERRM=SSERR/D FR=SSR/SERRM FC=SSR/SERRM FC=SSR/SERRM FRC=SSR/SERRM FRC=SSR/SERRM	BLE SUMS TABLE SUMS SO ROW FA SS. BLE SUMS SQUARED BSUM/FLOAT(NSUM) N1+N2)+R2S*R2S/(N2+N N1+N3)+C2S*C2S/(N2+N SR-SSC RSSC-SSRC ROWS,COLS,& TABLE OF CM (VE DROP CASE FRCM CO) GO TO 310	N4)-TSS N4)-TSS SUM3*SUM3/N3+SUM4	*SUM4/N4-1	TSS

```
DO 305 I=1.3
     X1=SQRT(F(I))*(1.-0.25/DF)/SQRT(1.+0.5*F(I)/DF)
     X2=1.0+X1*(CC1+X1*(CC2+X1*(CC3+X1*CC4)))
     X3=X2*X2*X2
     PF(I)=1.-1./X3
C CNT NON-SIGNIFICANT CASES - ROW, COL & TABLE
     IF(PF(I).LE.0.95) NSIG(I)=NSIG(I)+1
305 CONTINUE
C PRINT CASE PARAMETERS
     IF(LINE.LE.56) GO TO 307
     WRITE(6,200)DATE, I PAGE
     LINE=6
     IPAGE=IPAGE+1
307 WRITE(6,201)P,N,F,PF
     LINE=LINE+1
     CONTINUE
306
C CALC SIGNIFICANT CASES, PERCENTAGES, & PRINT SUMMARY
     ANC=NC
     DO 308 L=1,6,2
     M=L/2+1
     LSIG=NSIG(M)
     MSIG=NC-LSIG
     PRCT(L)=FLOAT(MSIG)*100/ANC
     PRCT(L+1)=FLOAT(LSIG)*100/ANC
     CONTINUE
     WRITE(6, 202) DATE, PRCT, NC
     STOP
                              1.7
     END
```

40

```
C ON120 ORAVECZ-NEWMAN HYPOTHESIS - NONSIGNIF DISPROP CASE
C MODIFIED FROM ON100 03-09-76 WD WHEATON
                                                 ROW FACTOR NOT
C DEFINITION - 2X2 CONTINGENCY TABLE
                                                 NECESSARILY BIGNIFICANT
 C CELL(1,1) EQU CELL(1)
   CELL(1,2) EQU CELL(2)
CELL(2,1) EQU CELL(3)
 C
    CELL(2,2) EOU CELL(4)
 C
       REAL*4 P(4), SUM(4), SUMS(4), F(3), PF(3), FSIG(2,6)
 C DEFN - MATRIX NSIG(2,3) CONTAINS COUNT OF NON-SIG F'S
     COL 1 CHI SO'D SIG
     COL 2 CHI SQ'D NON-SIG
 Ĉ
           ROW OF TABLE
     ROW 1
 C
            COL OF TABLE
     ROW 2
     ROW 3 TABLE
       INTEGER*4 N(4), SIG, NSIG(2,3), SCHI, DATE(2)
       EQUIVALENCE (SUM(1), SUM1), (SUM(2), SUM2), (SUM(3), SUM3),
      I(SUM(4), SUM4), (N(1), N1), (N(2), N2), (N(3), N3), (N(4), N4),
      2(F(1),FR),(F(2),FC),(F(3),FRC)
       DATA NSIG/6*0/, LTRN, LTRS/'N', 'S'/
      FORMAT('1',35X,'ON120 DRAVECZ & NEWMAN DISPROPURTIONAL CELL SIZES
  200
         ',4A2,T123, 'PAGE',13//
                  CELL SIZE RATIOS
      2 1
                                                   CELL POPULATION SIZE
      3
                       F VALUES
                                                       PROBABILITIES'/
      41
                                      (2,2) (1,1) (1,2) (2,1) (2,2)
      61
          (1.1)
                       COL
                                                        COL TABLE'/
      7
            ROW
                                      TABLE
                                               - ROW
                                     _____
      81
                                              . . .....
                       --- -
  201
       FORMAT(F8.5,3F9.5,1X,417,1X,3E12.4,1X,3F9.5,1X,A1)
       FORMAT( 'IONIZO DRAVECZ & NEWMAN DISPROPORTIONAL CELL SIZES 1,244
      1/// CHI SQ''D NON-SIG F TEST RESULTS (PERCENTS)'//
      210X, NON-SIG
                         SIG 1/
      310X,'----
      4' ROW ',2F11.2//
      5' COL
             1,2F11.2//
      6' TABLE', 2F11.2//
7/// CHI SQ''D SIG F TEST RESULTS (PERCENTS) *//
                       SIG
      910X, '----
      A' ROW ',2-11.2//
      B' COL ',2F11.2//
      C' TABLE', 2F11.2//
      D/// CASES CONSIDERED FOR EACH STATE CHI SQ'D =',14)
 C FIX TOTAL NUMBER OF CASES
       NC=1000
 C GET CURRENT DATE
 CALL TOATE(1, DATE)
C CONSTANT NEEDED LATER D1=2./9.=J.222222
        D1=0.222222
 C PROBABILITY EXPANSION CONSTANTS
       CC1=0.195854
        CC2=0.115194
        CC3=0,000344
        CC4=0.019527
  C NUMBER SIG & NON-SIG CASES CHI SQ'D
        NSCHT=0
        SCHI=0
C PAGE & LINE CHTS
```

MAIN

```
10/04/43
        LINE=100
        IPAGE=1
      . IY=9
 C GENERATE CELL SIZES (BETHEEN 10 AND 1000)
   306 NSUM=0
     x 00 300 I=1,3
        IX = IY
        CALL RANDU(IX, IY, A)
        IF (A.LT. J. 10) GU TO 301
        N(I)=A*100.
        NSUM=NSUM+N(I)
   300 CONTINUE
X C GENERATE N4 SO DISPROPORTIONAL
 X 302 IX=IY
      * CALL RANDU( IX, IY, A)
      X NA=A+10.+1.

    N4=N2*N3/N1+NA

      XNSUM=NSUM+N4
        SUMN=NSUM
  C CALC CHI SQUARED
      . CHI2A=N1*N4-N2*N3
        CHI2=SUMN*CHI2A*CHI2A/((N1+N2)*(N3+N4)*(N1+N3)*(N2+N4))
   TEST SIGNIFICANCE OF CHI SQ'D
     X IF(CH12.GT.1.320) GO TO 306
* C CHI SQ NON-SIG TEST FOR NC CASES

* IF (NSCHI-EQ-NC) GO TO 312

* C NOT ENDIGH ADD THIS ONE
FC NOT ENOUGH ADD THIS ONE
      ¥LS=2
      *NSCHI=NSCHI+1
       ⊀SIG=LTRN
 C GENERATE MEMBERS OF EACH CELL & CELL SUM
   313 TSUMS=0.0
        DO 303 I=1,4
        SUM(1)=0.0
        SUMS(1)=0.0
        P(I)=FLOAT(N(I))/SUMN
        L=N(I)
       EO 304 J=1,L
        IX=IY
       CALL RANDULTX, IY, A)
        SUM([)=SUM(])+A
        SUMS(I)=SUMS(I)+A*A
       CONTINUE
       TSUMS=TSUMS+SUMS(I)
  303 CONTINUE
 C CALC F STATISTICS
   CALC ROW, COL, & TABLE SUMS
     CALC ROW, COL, & TABLE SUMS SO ROW FACTOR SIGNIF
       91S=SUM1+SUM2
        P2S=SUM3+SUM4
       C1S=SUM1+SUM3
       C2S=SUM2+SUM4
       TABSUM=R1S+R2S
 C CALC ROW, COL, & TABLE SUMS SQUARED
        TSS=TARSUM*TARSUM/FLOAT(NSUM)
        SSR=R1S*R1S/(N1+N2)+R2S*R2S/(N3+N4)-TSS
        SSC=C1S*C1S/(N1+N3)+C2S*C2S/(N2+N4)-TSS
        SST=TSUMS-TSS
        SSCELL=SUM1*SUM1/N1+SUM2*SUM2/N2+SUM3*SUM3/N3+SUM4*SUM4/N4-TSS
```

10/04/43

```
SSRC=SSCELL-SSR-SSC
      SSERR=SST-SSR-SSC-SSRC
C CALC F VALUES FOR ROWS, COLS, & TABLE
      DF=NSUM-4
      SERRM=SSERR/DF
      FR=SSR/SERRM
      FC=SSC/SERRM
      FRC=SSRC/SERRM
      CONTINUE
C IF F(I) IS NEGATIVE DROP CASE FROM CONSIDERATION
      [F(FR.L1.0.0) GU TO 316
      [F(FC.LT.J.O) GO TO 316
      IF(FRCoLTs0o0) GO TO 316
C CALC PROBABILITIES FOR ROWS, COLS & TABLE
      D2=D1/DF
      CO 305 I=1,3
      X1=SQRT(F([))*(1.-0.25/DF)/SQRT(1.+0.5*F(I)/DF)
      X2=1.0+X1*(CC1+X1*(CC2+X1*(CC3+X1*CC4)))
      X3=X2*X2*X2*X2
      PF(I)=1.-1./X3
C CNT NON-SIG CASES OF F
      IF(PF(I).LE.O.95) NSIG(LS,I)=NSIG(LS,I)+1
 305 CONTINUE
C PRINT CASE PARAMETERS
      IF(LINE.LE.56) GO TO 307
      WRITE(3,200)DATE, IPAGE
      LINE=6
      IPAGE=IPAGE+1
      WRITE(3,201)P,N,F,PF,SIG
      LINE=LINE+1
 DO WE HAVE ENDUGH CASES OF SIG AND NON-SIG CHI YET
      IF (NSCHI.LT.NC) GO TO 306
C CALC & PRINT SUMMARY
C MATRIX FSIG(2,6) CONTAINS THE PERCENTS AS FOLLOWS
    COL 1
           PERCENT NON-SIG F'S
C
    COL 2 PERCENT SIG F'S
           ROW F NON-SIG CHI SQ'D
    ROW 1
    ROW 3 TABL F NON-SIG CHI SO'D
    ROW 4
           ROW SIG CHI SQ'D
    ROW 5
           COL SIG CHI SO'D
С
    ROW 6
           TAB SIG CHI SQ'D
 315 CN=NC
      K=2
      CO 314 I=1,6
      L=[-[[-1]/3*3
       [F(1.EQ.4) K=1
      TMP=FLOAT(NSIG(K,L))
       FSIGIT, IT=TMP/CN=100
      FSIG(2,1)=(CN-TMP)/CN*100.
      CONTINUE
      WRITE(3,202)DATE, FSIG, NC
      STOP
 C F(I) IS NEG DROP CASE
316 IF(SIG.EO.LTRS) SCHI=SCHI-1
       IF(SIG. FO.LTRN) NSCHI =NSCHI-1
       GU TD 306
       END
```

'G LEVEL 21

```
C MODIFIED FROM ON100 03-09-76 WD WHEATON ROW FACTOR SIGNIFICANT
C DEFINITION - 2X2 CONTINGENCY TABLE
C CELL(1,1) EQU CELL(1)
   CELL(1,2) EQU CELL(2)
С
   CELL(2,1) EQU CELL(3)
   CELL(2,2) EQU CELL(4)
      REAL*4 P(4), SUM(4), SUMS(4), F(3), PF(3), FSIG(2,6)
C DEFN - MATRIX NSIG(2,3) CONTAINS COUNT OF NON-SIG F'S
    COL 1 CHI SO'D SIG
    COL 2 CHI SQ'D NON-SIG
ROW 1 ROW OF TABLE
C
С
           COL OF TABLE
    ROW 2
    ROW 3 TABLE
      INTEGER*4 N(4), SIG, NSIG(2,3), SCHI, DATE(2)
      EQUIVALENCE (SUM(1), SUM1), (SUM(2), SUM2), (SUM(3), SUM3),
     1(SUM(4), SUM4), (N(1), N1), (N(2), N2), (N(3), N3), (N(4), N4),
     2(F(1),FR),(F(2),FC),(F(3),FRC)
      DATA NSIG/6*0/, LTRN, LTRS/'N', 'S'/
      FORMATI'1',35X, 'ON120 ORAVECZ & NEWMAN DISPROPORTIONAL CELL SIZES
     1
        ',4A2,T123,'PAGE',I3//
                 CELL SIZE RATIOS
                                                   CELL POPULATION SIZE
     3
                     F VALUES
                                                      PROBABILITIES!/
                   (1,2) (2,1)
                                                       (1,2) (2,1) (2,2)
     6
                                     (2,2)
                                                (1,1)
                                     TABLE
                                                      COL, TABLE'/
     8 4
     FORMAT(F8.5,3F9.5,1X,417,1X,3E12.4,1X,3F9.5,1X,41)
 201
      FORMAT( 11CM120 ORAVECZ & NEHMAN DISPROPORTIONAL CELL SIZES 1,244
     1/// CHI SQ''D NON-SIG F TEST RESULTS (PERCENTS)'//
210X,'NON-SIG SIG '/
     210X, NON-SIG
     310X, ---
                            ---1/
     4' ROW ',2F11.2//
5' COL ',2F11.2//
     6' TABLE',2F11.2//
     7/// CHI SQ''D SIG F TEST RESULTS (PERCENTS) 1//
     810X, NON-SIG
                      SIG '/
     910X,'----
     A' ROW ',2F11.2//
B' COL ',2F11.2//
     C' TABLE', 2F11.2//
     D/// CASES CONSIDERED FOR EACH STATE CHI SQ'D =',14)
C FIX TOTAL NUMBER OF CASES
      NC=1000
C GET CURRENT DATE
      CALL TOATE(1,DATE)
C CONSTANT NEEDED LATER C1=2./9.=0.222222
      D1=0.222222
C PROBABILITY EXPANSION CONSTANTS
      CC1=0.196854
      CC2=0.115194
      CC3=0,000344
      CC4=0.019527
C NUMBER SIG & NON-SIG CASES CHI SQ'D
      NSCHI=0
      SCHI=0
C PAGE & LINE CHTS
```

```
DATE = 76175
                                                                          10/34/32
                              MAIN
G LEVEL 21
         LINE= 100
         IPAGE=1
         IY=9
  C GENERATE CELL SIZES (BETWEEN 10 AND 1000)
         NSUM=0
   306
         DO 300 I=1,3
   301
         IX=IY
         CALL RANDUIIX, IY, A)
         IF(A.LT.0.10) GO TO 301
         N(I)=A*100.
         NSUM=NSUM+N(I)
         CONTINUE
    300
    GENERATE N4 SO DISPROPERTIONAL
X C
 X 302
        IX= IY
        CALL RANDU(IX, IY, A)
       NA=A*10.+1.
       X N4=N2*N3/N1+NA
       X NSUM=NSUM+N4
         SUMN=NSUM
  C CALC CHI SQUARED
         CHI2A=N1*N4-N2*N3
         CHI2=SUMN*CHIZA*CHIZA/((N 1+N 2)*(N3+N4)*(N1+N3)*(N2+N4)}
     TEST SIGNIFICANCE OF CHI SQ'D
         IF(CHI2.GT.1.320) GO TO 306
  C CHI SQ NON-SIG TEST FOR NC CASES
IF(NSCHI.EQ.NC) GO TO 312
  C NOT ENDUGH ADD THIS ONE
         LS≃2
         NSCHI=NSCHI+I
         SIG=LTRN
    GENERATE MEMBERS OF EACH CELL & CELL SUM
    313
         TSU4S=0.0
         00 303 I=1,4
         SUM( I )=0.0
          SUMS(I)=0.0
         P(I)=FLOAT(N(I))/SUMN
         L=N(I)
         DO 304 J=1,L
         IX=IY
         CALL RANDU(IX, IY, A)
   C FUR CELLS I AND 2 ADD FIVE TO EACH DATA POINT
         IF(I.LE.2) A=A+5
         SUM(I)=SUM(I)+A
         SUMS(I)=SUMS(I)+A*A
    304
         CONTINUE
         TSUMS=TSUMS+SUMS(1)
    303
         CONTINUE
   C CALC F STATISTICS
   C CALC ROW, COL, & TABLE SUMS
        CALC ROW, COL, & TABLE SUMS SO ROW FACTOR SIGNIF
          R1S=SUM1+SUM2
          R2S=SUM3+SUM4
          CIS=SUMI+SUM3
          C2S=SUM2+SUM4
          TABSUM=R1S+R2S
     CALC ROW, COL, S TABLE SUMS SQUARED
```

TSS=TABSUM*TABSUM/FLOAT(NSUM)

SSR=R1S*R1S/(N1+N2)+R2S*R2S/(N3+N4)-TSS SSC=CIS*CIS/(NI+N3)+C25*C25/(N2+N4)-T55 G LEVEL 21

10/34/32

```
SST=TSUMS-TSS
      SSCELL=SUM1*SUM1/N1+SUM2*SUM2/N2+SUM3*SUM3/N3+SUM4*SUM4/N4-TSS
      SSRC=SSCELL-SSR-SSC
      SSERR=SST-SSR-SSC-SSRC
C CALC F VALUES FOR ROWS, COLS, & TABLE
      DF=NSUM-4
      SERRM=SSERR/DF
      FR=SSR/SERRM
      FC=SSC/SERRM
      FRC=SSRC/SERRM
 500
      CONTINUE
C IF F(I) IS NEGATIVE DROP CASE FROM CONSIDERATION
      IF(FR.LT.0.0) GO TO 316
      IF(FC.LT.0.0) GO TO 316
      IF(FRC.LT.0.0) GO TO 316
C CALC PROBABILITIES FOR ROWS, COLS & TABLE
      D2=D1/DF
      00 305 I=1.3
      X1=SQRT(F(I))*(1.-0.25/DF)/SQRT(1.+0.5*F(I)/DF)
      X2=1.0+X1*(CC1+X1*(CC2+X1*(CC3+X1*CC4)))
      X3=X2*X2*X2*X2
      PF(I)=1.-1./X3
C CNY NON-SIG CASES OF F
      IF(PF(I).LE.O.95) NSIG(LS.I)=NSIG(LS.I)+1
 305
      CONTINUE
C PRINT CASE PARAMETERS .
      IF(LINE.LE.56) GO TO 307.
      HRITE(3,200)DATE, IPAGE ....
      LINE=6
      IPAGE=IPAGE+1
      WRITE(3,201)P,N,F,PF,SIG
      LINE=LINE+1
C DO WE HAVE ENDUGH CASES OF SIG AND NON-SIG CHI YET
     IF(NSCHILLT-NC) GO TO 306.
 312
 CALC & PRINT SUMMARY
C MATRIX FSIG(2,6) CONTAINS THE PERCENTS AS FOLLOWS
           PERCENT NON-SIG F'S
    COL 1
          PERCENT SIG F'S
C
C
    ROW 1
           ROW F NON-SIG CHI SQ'D
    ROW 2
C
           COL F NON-SIG CHI SQ'D
    ROW 3 TABL F NON-SIG CHI SQ'D
C
    ROW 4
           ROW SIG CHI SQ'D
¢
           COL SIG CHI SQ'D
    ROW 5
    ROW 6 TAB SIG CHI SQ'D
 315 CN=NC
                              .
      K=2
      DO 314 I=1.6
      L=I-(I-1)/3*3
      IF([.EQ.4] K=1
      TMP=FLOAT (NSIG(K,L))
      FSIG(1,1)=TMP/CN*1000
      FSIG(2,1)=(CN-TMP)/CN*100.
      CONTINUE
      WRITE(3,202)DATE, FSIG, NC
      STOP
C F(1) IS NEG DROP CASE
     IF(SIG.EQ.LTRS) SCHI=SCHI-1
      IF(SIG.EQ.LTRN) NSCHI=NSCHI-1
      GO TO 306
      END
```

```
* C ONIZO ORAVECZ-NEWMAN HYPOTHESIS - SIGNIF DISPROPORTIONAL CASE
                                                  ROW FACTOR NOT
NECCESSAMILY SIGNIFICANT
  C MODIFIED FROM ON100 03-09-76 WD WHEATON
   C DEFINITION - 2X2 CONTINGENCY TABLE
     CELL(1,1) EQU CELL(1)
  C
     CELL(1,2) EQU CELL(2)
  C
     CELL(2,1) EQU CELL(3)
  C
     CELL(2,2) FOU CELL(4)
        REAL*4 P(4),SUM(4),SUMS(4),F(3),PF(3),FSIG(2.6)
  C DEFN - MATRIX NSIG(2,3) CONTAINS COUNT OF NON-SIG F'S
       COL 1 CHI SO'D SIG
       COL 2 CHI SQ'D NON-SIG
  C
  C
       ROW 1 ROW OF TABLE
            COL OF TABLE
       ROW 2
       ROW 3
             TABLE
         INTEGER*4 N(4), SIG, NSIG(2,3), SCHI, DATE(2)
        EQUIVALENCE (SUM(1), SUM1), (SUM(2), SUM2), (SUM(3), SUM3),
       1(SUM(4), SUM4), (N(1), N1), (N(2), N2), (N(3), N3), (N(4), N4),
       2(F(1),FR),(F(2),FC),(F(3),FRC)
        DATA NSIG/6*0/, LTRN, LTRS/'N', 'S'/
   200
        FORMAT("1",35X, "ON120 ORAVECZ & NEWMAN DISPROPORTIONAL CELL SIZES
           ',4A2,T123, 'PAGE',13//
       1
                                          .....
                   CELL SIZE RATIOS
                                                    CELL POPULATION SIZE
       3
                        F VALUES
                                                        PROBABILITIES"/
       41
       61
            (1,1)
                     (1,2)
                              (2,1)
                                        (2,2)
                                                 (1,1)
                                                                       12,21
                                                         (1,2)
                                                                (2,1)
       7 .
            ROM -
                    COL
                                      TABLE
                                                        COL
                                                  ROP
                                                                    TABLE /
       FORMAT(F8.5,3F9.5,1X,4I7,1X,3E12,4,1X,3F9.5,1X,A1)
    201
        FORMATI'IONIZO ORAVECZ & NEWMAN DISPROPORTIONAL CELL
       1/// CHI SQ!'D NON-SIG F TEST RESULTS (PERCENTS)'//
210X, NON-SIG SIG /
       4 ROW
               ',2F11.2//
       5' COL
              ',2F11.2//
       6' TABLE', 2F11.2//
 7/// CHI SQ''D SIG F TEST RESULTS (PERCENTS) 1//
       A' ROW ',2F11.2//
       B. COF
               ',2F11.2//
       C' TABLE', 2F11,2//
       D/// CASES CONSIDERED FOR EACH STATE CHI SQ D = 1,14) ..
  C FIX TOTAL NUMBER OF CASES
  C GET CURRENT DATE
        CALL TDATE(1,DATE)
  C CONSTANT NEEDED LATER D1=2./9.=0.222222
        D1=0.222222
 C PROBABILITY EXPANSION CONSTANTS
        CC1=0.196854
        CC2=0.115194
        CC3=0.000344
        CC4=0.019527
  C NUMBER SIG & NON-SIG CASES CHI SQ O
        NSCHI=0
 . .
       SCHI=0
  C PAGE & LINE CHTS
```

MAIN

11/06/46

```
LINE=100
        IPAGE=1
        1Y=9
  C GENERATE CELL SIZES (BETWEEN 10 AND 1000)
   306 NSUM=0
     X 00 300 I=1,4
   301 IX=IY
        CALL RANDU(IX, IY, A)
        IF(A.LT.0.10) GO TO 301
                                                MA SKALL
        N(I)=A*100.
        NSUM=NSUM+N(I)
   300 CONTINUE
       SUMN=NSUM
  C CALC CHI SQUARED
      , CHI2A=N1*N4-N2*N3
        CHI2=SUMN*CHIZA*CHIZA/((N1+N2)*(N3+N4)*(N1+N3)*(N2+N4))
  C TEST SIGNIFICANCE OF CHI SQ'D
     X IF(CHI2.LE.3.841) GO TO 306
XC CHI SQ'D SIG TEST FOR NC CASES
    -X IF(SCHI.EQ:NC) GO TO 312
FC NOT ENDUGH ADD THIS ONE
     X LS=1
X SCHI=SCHI+1
      * SIG=LTRS
  C GENERATE MEMBERS OF EACH CELL & CELL
   313
       TSUMS=0.0
       DO 303 I=1.4
       SUM(1)=0.0
        SUMS(1)=0.0
       P(I)=FLOAT(N(I))/SUMN
        L=N(I)
       DO 304 J=1,L
                                   ·r .
        IX=IY
       CALL RANDU(IX. IY.A)
        SUM(I)=SUM(I)+A
       SUMS(I)=SUMS(I)+A+A
       CONTINUE
       -TSUMS=TSUMS+SUMS(I)
  303
       CONTINUE
 C CALC F STATISTICS
 C CALC ROW, COL, & TABLE SUMS
     CALC ROW, COL, & TABLE SUMS SO ROW FACTOR SIGNIF
       R1S=SUM1+SUM2
       R2S=SUM3+SUM4
       C1S=SUM1+SUM3
       C2S=SUM2+SUM4
       TABSUM=R1S+R2S
 C CALC ROW, COL, & TABLE SUMS SQUARED
       TSS=TABSUM+TABSUM/FLOAT(NSUM)
       SSR=R1S*R1S/(N1+N2)+R2S*R2S/(N3+N4)-TSS
       SSC=C15*C15/(N1+N3)+C25*C25/(N2+N4)-TSS
       SST=TSUMS-TSS
       SSCELL=SUM1*SUM1/N1+SUM2*SUM2/N2+SUM3*SUM3/N3+SUM4*SUM4/N4-TSS
       SSRC=SSCELL-SSR-SSC
        SSERR=SST-SSR-SSC-SSRC
 C CALC F VALUES FOR ROWS, COLS, & TABLE
       DF=NSUM-4
       SERRM=SSERR/DF
FR=SSR/SERRM
```

FC=SSC/SERRM FRC=SSRC/SERRM 500 CONTINUE C LE E(1) IS NEGATIVE DROP CASE FROM CONSIDERATION IF(FR.LT.0.0) GO TO 316 IF(FC.LT.0.0) GO TO 316 IFIERCALTADADA GO TO 316 C CALC PROBABILITIES FOR ROWS, COLS & TABLE D2=D1/DF DO 305 I=1.3 X1=SQRT(F(I))*(1.-0.25/DF)/SQRT(1.+0.5*F(I)/DF) X2=1.0+X1*(CC1+X1*(CC2+X1*(CC3+X1*CC4))) X3=X2*X2*X2*X2 PF(I)=1--1-/X3 C CNT NON-SIG CASES OF F IF(PF(I).LE.O.95) NSIG(LS.I)=NSIG(LS.I)+1 CONTINUE C PRINT CASE PARAMETERS IF(LINE.LE.56) GO TO 307 WRITE(3,200)DATE, IPAGE LINE=6 IPAGE=IPAGE+1 307 WRITE(3,2011P,N,F,PF,SIG LINE=LINE+1 DO WE HAVE ENOUGH CASES OF SIG AND NON-SIG CHI YET X312 IF(SCHI-LT.NC) GO TO 306 184 15 18 8 -C CALC & PRINT, SUMMARY C MATRIX FSIG(2,6) CONTAINS THE PERCENTS AS FOLLOWS COL 1 PERCENT NON-SIG F'S COL 2 PERCENT SIG F'S ć. ROW 1 ROW F NON-SIG CHI SO'D ROW 2 COL F NON-SIG CHI SQ'D C ROW 3 TABL P NON-SIG CHI SQID C ROW 4 ROW SIG CHI SO'D
ROW 5 COL SIG CHI SO'D
ROW 6 TAB SIG CHI SO'D C 315 CN=NC DO 314 J=1,6 L=I+(I-1)/3*3 IF(I.EQ.4) K=1 TMP=FLOAT(NSIG(K,L)) FSIG(1, I)=THP/CN+100. FSIG(2, 1) = (CN-THP) / CN+LQ0 314 CONTINUE WRITE(3,202)DATE, FSIG.NC STOP C F(I) IS NEG DROP CASE 316 IF(SIG.EQ.LTRS) SCHI=SCHI-1
IF(SIG.EQ.LTRN) NSCHI=NSCHI-1 GO TO 306

1

```
MAIN
C LEVEL 21
                                                                      11/40/57
 C CN12C DEAVECZ-NEWMAN HYPCTHESIS - SIGNIF DISPROPORTIONAL CASE
 C MCDIFIED FREM CNICO 03-05-76 MD WHEATON ROW FACTOR SIGNIFICANT
 C DEFINITION - 2X2 CONTINGENCY TABLE
                                                                     and are a few or the second
    CELL(1),11 EQU CELL(1)
    CELL(1,2) FQU CELL(2)
    CELL(2,1) ECU CELL(3)
    TELL(2.2) EQU CFLL(4)
       REAL *4 P(4), SUM(4), SUMS(4), F(3), PF(3), FSIG(2,6)
 C DEFN - MATRIX NSIG(2,3) CENTAINS COUNT OF NON-SIG F'S
         1 CHI SCIE SIG
     CCL 2 CHI SC'E NON-SIG
     POW 1 RCW CF TABLE
     RCW 2 CCL CF TABLE
       INTEGER#4 N(4), SIG, NSIG(2,3), SCHI, DATE(2)
       EQUIVALENCE (SUM(1), SUM1), (SUM(2), SUM2), (SUM(3), SUM3),
      1(SUM(4), SUM4), (N(1), N1), (N(2), N2), (N(3), N3), (N(4), N4),
      2(F(1), FR), (F(2), FC), (F(3), FRC)
       CATA NSIG/6+0/, LTRN, LTRS/!N', "S'/
      FCRMAT('1',35x, 'CN120 CRAVECZ & NEWMAN DISPROPERTIONAL CELL SIZES
      1 ',4A2,T123,'P4GE',I3//
      21
             CELL SIZE RATIOS
                                                   CELL POPULATION SIZE
      3
                       F VALUES
                                                     PROBABILITIES'/
                   (1,2) (2,1) (2,2)
      C' (1,1) (1,2) (2,1) (2,2) (1,1) (1,2) (2,1) (2,2)
7 ROW CCL TABLE ROW COL TABLE'/
  201 FORMAT (F8.5, 3F9.5, 1x, 4f7, 1x, 3E12.4, 1x, 3F9.5, 1x, A1)
       FORMATI ICN120 ORAVECT & NEWNAN DISPROPERTICNAL CELL SIZES 1.244
      1/// CHI SQ''D NCK-SIG F TEST RESULTS (PERCENTS)'//
210x.'NCK-SIG SIG '/
      310x, '----
      4' PCW '.2F11.2//
5' CCL '.2F11.2//
      6' TABLE', 2F 11.2//
      7/// CHI SQ''D SIG F TEST RESULTS (PERCENTS)'//
      810X, 'NCN-SIG SIG '/
      510x, -----
      4' 7CW ',2F11.2//
      B' CCL ',2F11.2//
      C' 743LE1.2711.2//
      DI// CASES CONSIDERED FOR EACH STATE CHI SQ'ID = 1,14)
 C FIX TOTAL NUMBER OF CASES
       N:C = 2
  FIX NUMBER OF CASES IN CEPUC
       ICNI= >
 C GET CLERENT CATE
       CALL TEATE(1, CATE)
 C CONSTANT WEEDED LATER D1=2./9.=0.222222
 C PROBABILITY EXPANSION CONSTANTS
       CC1= 1.196854
       CC2=1.115194
       CC3=C.CCC344
       GC4=7.019527
 C NUMBER SIG & NON-SIG CASES CHI SCID
       150+ I=C
```

The state of the s

```
SCHI=0
    PAGE & LINE CHTS
        LINE=1(0
        IPAGE=1
        IY=9
  C GENERATE CELL SIZES (BETHEEN 10 AND 1900)
   306
       V Z F.N = U
        DE 300 I=1.4
        IX=IY
   301
        CALL RANGU(IX, IY, A)
        IF (A.LT. J. 10) GC TC 301
        N( I) = A + 1 GO.
        NSUM=NSUM+N(I)
   300
        CONTINUE
        SUMN = N SUM
  C CALC CHI SQUARED
        CHI24=K1*N4-N2*N3
        CHI2=SUMN+CHI2A+CHI2A/((N1+N2)+(N3+N4)+(N1+N3)+(N2+N4))
 C TEST SIGNIFICANCE OF CHI SQ'C
  C CHI SG'D SIG TEST FOR NO CASES
        IF(SCHI.EQ.NC) GC TC 312
C NOT ENCUGH ACC THIS CHE
        LS=1
        SCHI=SCHI+1
         SIG=LTRS
  C GENERATE MEMPERS OF EACH CELL & CELL SUM
        TSUMS=C.C
   313
         CC 303 I=1.4
         0.0=[1]MU2
. s - W
          SUMS(1)=0.0
         P(I)=FLOAT(N(I))/SUMN
         L=N(I)
         DC 304 J=1,L
         IX=IA
         CALL RANGULIX, IY, A)
   C FOR CELLS 1 AND 2 ACC FINE TO EACH DATA POINT
         IF ( I . LE . 2 ). A = 4+5
         SUP(I)=SUP(I)+A
         SUMS(I)=SUMS(I)+A+A
         CCNTINLE
    304
         TSUMS=TSUMS+SUMS(I)
3. 303 CONTINUE
     CALC F STATISTICS.
   C CAIC SCH, CEL & TABLE SCHS
       CALC RCW, CCL, & TABLE SUMS SC RCW FACTOR SIGNIF
         RIS=SUMI+SUM2
         R2S=SU#3+SUM4
         C1S=SUM1+SUM3
         C2S=SUP2+SUP4
          TABSUM=R1S+R2S
    C CALC RCW.CCL, & TABLE SUMS SQUARED
          TSS=TARSUM*TABSLM/FLCAT(KSUM)
         SSR=R15*R15/(N1+N2)+R25*R25/(N3+N4)-TS5
          SSC=C15+C15/IN1+N31+C25+C25/IN2+N41-TSS
          SST=TSUMS-TSS
          SSCELL=SUM1*SUM1/N1+SUM2*SUM2/N2+SUM3*SUM3/N3+SUM4*SUM4/N4-TSS
          SSEFR=SST-SSR-SSC-SSRC
  G LEVEL 21
                              MAIN
                                                DATE = 77056
                                                                      11/40/57
    C CALC F VALLES FOR PCHS, CCLS, 6 TABLE
          CF=NSUM-4
          SERF #= SSER9/DF
```

```
51.
```

```
EQ=SSR/3=RRM
        FC=SSC/SERRM
        FRC=SSRC/SERRM
       CONTINUE
  C IF F(I) IS NEGATIVE CREP CASE FROM CONSIDERATION
        [=(=0.11.0.3) GC TC 316
        IF(FC.LT.G.G) GC TC 316
        IF(FRC.LT.0.0) GC TC 316
    CALC PROBABILITIES FOR ROWS .COLS & TABLE
        12=51/EF
        nc 205 I=1.3
        x1=SORT(F(I))*(1.-0.25/CF)/SCRT(1.+C.5*F(I)/DF)
        X2=1.0+X1*(CC1+X1*(CC2+X1*(CC3+X1*CC4)))
        x3'=X2+X2+X2
        PF(I)=1.-1./X3
  C CAT NON-SIG CASES OF F
        [F(PF(I).LF.0.95) NSIG(LS,I)=NSIG(LS,I)+1
       CENTINUE
  C PRINT CASE PARAMETERS
        IF(LINE.LE.56) GC TC 3C7
        WRITE(3,200)DATE, IPAGE
        LINE=6
        IPACE=IPACE+1
307
       WRITE(2,201)P,N,F,PF,SIG
       LINE=LINE+1
  C CO WE HAVE ENOUGH CASES OF SIG AND NON-SIG CHI YET
   312 IF(SCHI.LT.NC) GC TC 3C6
  C CALC & PRINT SUMMARY
  C MATRIX FSIG(2,6) CONTAINS THE PERCENTS AS FOLLOWS
            FERCENT NON-SIG FIS
      COL 2 PERCENT SIG F'S
  C
     ROW 1 RCW F NON-SIG CHI SQ'D
  C
                                             RCH 3 TABL F NCN-SIG CHI SQ'C
  C
     ROW 4 RCW SIG CHI SC'D
     ROW 5 CCL SIG CHI SC'C
  315 CN=NC
       K=2
       CC 314 I=1,6
       L=I-(I-1)/3*3
       IF ( I . E C . 4 ) K= 1
       TMP=FLCAT (NSIG(K,L))
       FSIG(1,1)=TMP/CN+1CC.
       FSIG(2.1)=(CN-TMF)/CN+160.
       CCNTINUE
       WRITE(3,202)DATE, FSIG, NO
       STEP
 C F(I) IS NEC DROP CASE
  316 IF(SIG.EC.LTRS) SCHI=SCHI-1
       IF(SIG. EC.LTRN) NSCHI = NSCHI-1
       CC TC 306
       CERLE UNIT(2)
       AT 204
       PISFLAY I,A
       AT 500
                                                                    11/40/57
                                               DATE = 77056
G LEVEL
                            MAIN
       CISPLEY TSUYS, PIS, RZS, CIS, CZS, TABSUM, TSS, SSR, SSC, SST, SSCELL, SSRC,
      15SERR, CG, SERRM, FR, FC, FRC
       ICAT=ICAT+1
       IF ( ICNT GT . 2) STCP
```

SHRINKAGE IN R² AND UNBIASED ESTIMATES OF TREATMENT EFFECTS USING ω

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Abstract

The amount of variance accounted for by treatment can be estimated with Ω^2 or with R^2 (symbolized as R_c^2 after a shrinkage formula has been applied). Monte Carlo methods were employed to compare Ω^2 , R_c^2 , and R^2 in terms of bias and precision. R_c^2 and Ω^2 produced estimates which were negligibly biased. The bias in R^2 , while consistently positive, decreased as sample size increased and was too small to be of practical importance when $n\geq 50$. Ω^2 , R_c^2 and R^2 were all most precise with large samples and least precise when treatment effects were moderate in magnitude.

Presented at A.E.R.A., New York, NY, April, 1977.

Shrinkage in \mathbb{R}^2 and Unbiased Estimates of Treatment Effects Using \mathbb{G}^2

William Hays (1963) encouraged investigators to provide estimates of the magnitude of treatment effects in addition to the statistics and probability levels which are customarily reported in analysis of variance. He offered omega squared (Ω^2) as an unbiased estimator of the parameter eta squared (η^2).

$$\omega^2 = \frac{SS_B - (J-1)MS_{\omega}}{SS_T + MS_{\omega}}$$

 $SS_{\tau} = sum of squares total$

 $SS_{R} = sum of squares between groups$

MS = mean of squares within groups

J = number of groups

and

$$\eta^2 = \frac{\sigma^2 - \sigma^2}{y} \frac{\sigma^2}{\varepsilon}$$

 σ_y^2 = variance of the dependent variable

 σ_{ε}^2 = the common homogeneous variance of the Y_{ij} about y_{j}

 η^2 = a population measure of the magnitude of treatment effects relative to the total variance in the experiment

Carroll and Nordholm (1975) have demonstrated that another estimate of η^2 (epsilon squared) developed earlier by Kelley (1935)

is as accurate as ω^2 . Nevertheless ω^2 appears to be most popular among researchers who use analysis of variance.

Researchers who use regression analysis for testing the same hypotheses tested in analysis of variance (e.g., McNeil, Kelly, and McNeil, 1975; Namboodiri, Carter and Blalock, 1975) use the squared multiple correlation coefficient (R^2) to estimate the proportion of variance accounted for by treatment (i.e., η^2). Because R^2 is positively biased a shrinkage formula is commonly used to provide a value of R^2 corrected for bias (R_c^2).

$$R_c^2 = 1 - (1-R^2) \frac{(N-1)}{N-k-1}$$

 $R_c^2 = R^2$ after correction for bias

N = number of subjects

k = number of independent variables

In the past, the selection of $R_{\rm c}^2$ or $\hat{\omega}^2$ to estimate η^2 has been determined by the researcher's preference for traditional analysis of variance or regression analysis. Because no one has compared these statistics in terms of bias and precision, no evidence is available for selection on the basis of accuracy. The primary purpose of this study, therefore, is to compare the sampling distributions of R^2 , $R_{\rm c}^2$, and $\hat{\omega}^2$ in terms of bias and precision.

Procedure

Using Monte Carlo methods, the study was conducted in the context of a three level, one way analysis variance. It was assumed the results would generalize directly to higher order analysis of variance. The values of η^2 selected were .00, .05, .15, .40. .75, and .90. Sample sizes ranged from N=30 (10,10,10) to N=600 (200, 200,200). Error terms were randomly selected from normal populations with homogeneous variances. Carroll and Nordholm (1975) studied the effect of violating the assumptions of normality and homogeneity when estimating η^2 using δ^2 . The reader interested in this problem is referred to their work. For each value of η^2 and for each sample size 1000 simulated experiments were conducted. Data were generated by the pseudorandom number generator in the IBM scientific package.

Results

Bias. For each value of η^2 and for each sample size the mean and standard error (SE) were calculated for R^2 , R_c^2 , and Ω^2 (Table 1). R_c^2 and Ω^2 produced estimates of η^2 which were negligibly

Insert Table 1 about here

biased. The bias in \mathbb{R}^2 , while consistently positive, decreased as sample size increased and was too small to be of practical importance

when n>50.

Precision. As reflected in the standard errors, the imprecision of all three statistics decreased as sample size increased. Imprecision was greatest in the middle of the range of η^2 (i.e., for η^2 =.15 and η^2 =.40). For small sample sizes R^2 was very slightly, yet consistently more precise than R^2 and Ω^2 .

Discussion

Any attempt to pinpoint a tendency in R_c^2 or Ω^2 to be positively or negatively biased, based upon the present data, would probably be misleading. The mean values of R_c^2 and Ω^2 always fell within two SEs of the population value (η^2) and 92% of the time both estimates were within one standard error of η^2 . The mean value of Ω^2 never differed from the population value by more than one SE. By these standards Ω^2 is slightly less biased than R_c^2 , however, this conclusion is overshadowed by the tendency of both measures to yield accurate estimates in terms of bias.

When Hays developed ω^2 he stressed the importance of estimating the magnitude of treatment effects when sample sizes were large. "Virtually any study can be made to show significant results if one uses enough subjects, regardless of how nonsensical the content may be." It is indeed ironic that the use of ω^2 (or

 R_c^2) instead of the familiar R^2 is least necessary when sample size is large. In this case the estimates of experimental effects using R^2 show only negligible bias. In the present study the mean value of R^2 ($n\geq 50$) never differed from n^2 by more than one standard error. This degree of bias should not concern most applied researchers. In addition, R^2 is routinely produced by many packaged computer programs and consequently is more readily available than R_c^2 and Ω^2 .

In conclusion, it appears that R_c^2 and Ω^2 may serve equally well in estimating the magnitude of experimental effects. Both are superior to R^2 in this regard when n<30. For large samples R^2 shows little bias and in many circumstances may be sufficient as an estimate of Ω^2 .

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Table 1 Means and Standard Errors (SE) of the Multiple Correlation Coefficient (\mathbb{R}^2) Omega Squared (\mathbb{Q}^2), and the Corrected Multiple Correlation Coefficient (\mathbb{R}^2) for Each Condition

						Et a	Squared	(η ²)						
impla	Estimates of	.00		.1	.05		.15		.40		.75		.90	
size	η2	x	SE	x	SE	x	SE	x .	SE	x	SE	x	SE	
	R ²	.069	.065	.116	.093	.209	.117	.443	.118	.771	.059	.909	.024	
1.0	.62	.000	.068	.049	.097	.147	.123	.394	.125	.748	.064	.899	.017	
	R ² _c	.000	.070	.051	.099	.150	.126	.402	.126	.754	.063	.902	.026	
	R ²	.023	.022	.070	.048	.167	.068	.411	.073	. 755	.037	.903	.015	
30	42	.000	.023	.049	.049	.146	.069	.395	-075	.748	.038	.899	.015	
	12 C	.000	,023	.049	.049	-148	.070	.397	.075	.750	.037	.900	.015	
	22	.013	.014	.063	.035	.161	.051	.408	.054	.753	.027	.901	.011	
30	6 ²	.000	.014	.050	.036	. 149	.051	.398	.055	.749	.027	.899	.011	
	1 _c ²	.029	.014	.023	.037	.126	.053	.382	.056	.743	-028	.897	.011	
						•				*				
	R ²	.007	.007	.057	-024	.157	.036	.405	.039	.753	.020	.901	.000	
	6 ²	.000	.007	.051	.024	.151	.036	.401	.039	.750	.020	.900	.006	
	R2 .	.014	.007	.038	.025	.139	.037	.393	.040	.748	.020	.899	.008	
	12	.004	.004	.055	.020	-154	.030	.404	.032	.752	.016	.901	.007	
1.50	6 ²	.000	.004	.050	.020	-150	.030	.401	.032	.751	.016	.900	.007	
	R2	.000	.004	.050	.020	.151	.030	.401	.032	.751	.016	.901	.007	
	12	.003	.003	.054	.017	.154	.026	-403	.028	.752	.014			
200	62	.000	.003	.050	.017	.151	.026	.401	.028	.751		.901	.006	
	R2	.000	.003	.050	.017	.151	.026	.401	.028	.751	.014	.900 .901	.006	

THE USE OF MULTIPLE REGRESSION ANALYSIS IN PREDICTING SUCCESS IN THE COUNSELING PRACTICUM *

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Abstract... The present exploratory study investigated the relationship between several predictor variables and the criterion of success in the counseling practicum among 93 recent graduates of a counselor education program. The investigation revealed that the best predictor of success in the counseling practicum was the square of the graduate grade point average (ggpa²). This suggests the possibility of a curvilinear relationship between this predictor and the criterion. The interaction of female by Miller Analogies Test score (MAT) and the single variable of undergraduate grade point average (Ugpa) also appeared early in the equation. Type of undergraduate institution, type of graduate degree earned, and sex as a single independent variable demonstrated little relationship to the criterion.

Introduction

The counseling practicum in most counselor education programs is conceived as a comprehensive experience in which the counselor education student is asked to demonstrate his or her ability to counsel in a practical sense, while using the methods and techniques that he or she has acquired in previous courses. It is a pre-service experience which normally occurs after substantive course work in counselor education has been completed, but before the student is certificated as a practicing counselor.

While one's rating in the counseling practicum may bear questionable relationship to one's ultimate success in the counseling field, the counseling practicum may be a fairly good barometer of the student's current level of achievement in the practical aspects of counseling, and an indicator of potential success in the field, if one assumes minimum bias in the subjective judgements of the practicum supervisor.

The present study is concerned with determining possible predictor variables that will be useful in predicting success in the counseling practicum.

A selected review of recent literature reveals some studies which are relevant to

^{*} non-reviewed

the present study.

James and Dumas (1976) examined college grade point average as a predicator of teaching competency and found a positive relationship between grade point average and competency ratings of student teachers. The authors emphasized that low risk students tended to have lower overall grades, as well as lower student teaching competency ratings.

Richards' (1974) study sought to predict performance in a combined undergraduate and medical education program. He found that the best predictor for a given criterion variable was previous standing on that same variable, and that academic performance in the program was largely independent of other criteria.

A later study by Wallace and Schwab (1976) compared five models which were used to predict graduate admission committee decisions. These investigators found that grade point average and Graduate Record Examination score tended to be weighted about the same from one model to another.

The studies cited above investigated linear relationships. However, the present study attempted to extend beyond the investigation of linear relationships and to explore curvilinear relationships through squared variables.

The present exploratory study investigated possible predictor variables for the criterion of success in the counseling practicum. The independent variables included type of undergraduate institution, sex, type of graduate degree earned, undergraduate grade point average (ugpa) graduate grade point average (ggpa) and Miller Analogies test score, (MAT). In addition, the interaction of several of the above variables was included. Specific interaction variables were: type of graduate degree by MAT; sex by ugpa, sex by ggpa, sex by MAT. Also, ugpa, ggpa, and MAT were squared in order to determine if curvilinear relationships existed.

Thus, the purpose of the present investigation was to examine possible predictors of counseling practicum success, while using a multiple regression approach. The intent was to derive a regression equation which would be useful in a replicative study.

Methods and Procedures

The present study was completed with 93 subjects who recently received the Master of Science in Education or Master of Arts in Education degree in the area of counseling from a large urban, midwestern university. The subjects, 54 females and 39 males, were randomly selected from the complete lists of recent graduates, and any subject with missing information, such as MAT score was excluded from the study. Forty-one of the subjects received the M.A. degree in Education, while the remaining 52 received the M.S. degree in Education. Type of undergraduate institution included: (1) the home institution, (2) other public institutions within the state, (3) private institutions within the state, and (4) public and private institutions outside of the state.

The subjects were divided into groups of "most successful" and "least successful" on the basis of final ratings which were assigned by the practicum supervisors. These two classifications were used as the criterion.

<u>Data Analysis</u>

The data were analyzed by the use of the Statistical Package for the Social Sciences (SPSS) multiple regression subprogram (Klecka, Nie and Hull, 1975). Input data included the independent and dependent variables enumerated above. The SPSS program computed a sequence of multiple linear regression equations in a stepwise manner. At each step the independent variable which made the greatest reduction in the error sum of squares was added to the regression equation. The results are

presented in the following section. The present study was completed as ex post facto research, and bears the limitations normally associated with such research (Kerlinger, 1973).

Results

The findings reveal that the predictor variables in the full model controlled 32.3 percent of the total variance. As indicated in Table 1 below, $ggpa^2$ accounted for most (23.7 percent) of the controlled variance. The interaction variable of female by MAT was nexted added to the regression equation to increase the R^2 by 2.3 percent. Ugpa was entered on step three, followed by $ugpa^2$. MAT² was added at step five to raise the R^2 to .295.

Beyond step five, additional variables were added to the regression equation in the following order: MAT, female, male by ugpa, ggpa, type of undergraduate institution, and male by ggpa. At this point the F- level became insufficient for further computation.

Newman (1973) pointed out that "multiple correlations (R) tend to be biased upward..." and that ... "R tends to be higher in the sample than in the population from which the sample is drawn." In order to correct this condition, he suggests the use of shrinkage estimates. This was not done in the present study, because of its exploratory nature. However, in a replicative study it will be important to make use of shrinkage estimates.

<u>Discussion</u> and Conclusions

As indicated above, graduate grade point average (squared) accounted for most of the variance in the regression models. This finding is somewhat similar to those of James and Dumas, who found a positive linear relationship between gpa and competency ratings of student teachers. However, while James and Dumas found linear relationships, the present study appears to reveal a curvilinear relationship between ggpa² and counseling practicum rating.

The interaction variable of female by MAT and the single variable of ugpa were also presented early in the regression equation. This in part seems consistent with the study by Wallace and Schwab, who found consistency in the weighting of undergraduate gpa and Graduate Record Examination score, when they tried to predict graduate admissions committee decisions. It is pointed out here that the primary bases for graduate school admission among students in the present study was undergraduate grade point average and MAT score.

The Richards study concluded in essence that the best predictor for a criterion variable was previous standing on that variable prior to admission to the desired program. This suggests that characteristics which practicum supervisors seek to develop should be sought in preliminary screening devices when students initially apply for counselor enucation programs.

Conclusively, while the present study did not generate a prediciton equation which is generalizable to other populations, it provided additional insight on ways of predicting success in the counseling practicum, by introducing the possibility that a second degree curvilinear relationship exists when ggpa² is introduced in a regression equation utilzing counseling practicum rating as the criterion. This investigator plans a replicative study to explore this concept further.

TABLE 1
Stepwise Multiple Regression Analysis for Selected Predictors of Counseling Practicus Success

Step	Predictor Variables	Multiple R			_R 2	Increase in R	
Restricted m	odeis						
1	ggpa ²	.487	*		.237		
2.	ggpa ² , female by MAT	.510	*		.260	.023	
3.	ggpa ² , female by MAT ugpa	. 525	*		.275	.016	
4.	ggpa ² , female by MAT ugpa, ugpa ² , MAT ²	.533 .538	*		.284 .290	.009 .006	
5.	ggpa ² , female by MAT ugpa, ugpa ² , MAT ²	. 538	*		.290	.006	
Full Model							
11	gopa ² , female by MAT, ugpa, ugpa ² , MAT ² , MAT, Female, Male by ugpa ggpa, type institution,						
	male by ggpa	.568	*		.323	.030	

^{*} p < .001

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RELATIONSHIPS BETWEEN RESULTS OBTAINED ON THE ERTL MACHINE AND THE WECHSLER INTELLIGENCE SCALE FOR CHILDREN (WISC)

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ABSTRACT

The purpose of this study was to examine relationships between the neural efficiency (NE), symmetry, and time difference (TD) scores on the Ertl machine and WISC scale scores for a group of 22 normal children and a group of 22 children with suspected learning disabilities, all ranging from 8 to 10 years of age. Multiple linear regression techniques were used to analyze the data. Some statistically significant relationships did occur between Ertl machine scores and WISC-V, WISC-P, and WISC-F scale scores for groups 1 and 2. Results supported Ertl's findings that normals and children with learning disabilities (LDs) would have similar NE scores (learning potential). Several symmetry scores (Hemispheric synchronization) and WISC scores correlated significantly in positive directions for both groups. Significant differences occurred between the TD scores (indicator of LDs) but results were in direct contrast to Ertl's claim since group 1 (normals) obtained higher mean scores than group 2.

REVIEW OF LITERATURE

The WISC instrument usually correlates consistently well with other measures of intelligence and has been widely used for diagnosing Children with Learning Disabilities (CLDs) (Sattler, 1974; Coleman & Rasof, 1963).

Results of WISC scores have indicated that CLDs often obtain higher WISC-P scores than WISC-V scores. Studies by Rourke, Young, and Flewelling (1971),

Wells (1970), and Ackerman, Peters, and Dykman (1971) have concluded that this may occur because CLDs usually have serious reading problems and faulty attention.

Other researchers (Meier, 1970; Kershner & Kershner, 1973; Sperry, 1975) supported the conclusion that CLDs on WISC scores (WISC-P greater than WISC-V) may be due to asymmetry of the brain's two hemispheres. Apparently these children have hemispheric cross integration difficulties which result in problems of general behavior and in academic tasks. Numerous experiments have demonstrated that the two hemispheres of the brain function differently with respect to the kinds of information each hemisphere stores and processes (Milner, 1967; Rosenfield & Klivington, 1975; Delgado, 1975; Sperry, 1975; Gardner, 1975). Studies generally support the conclusion that the left hemisphere is highly verbal and mathematical, performing with computer-like sequential logic, and the right hemisphere is instrumental in high-order integrative visual-spatial activities and cannot yet be simulated by computers. Pines (1973) has reported on new experimental methods being used whereby individuals can learn to integrate the hemispheres of the brain more effectively or to rely more heavily on one hemisphere than the other. This type of training may prove particularly useful for CLDs.

Much remains to be learned about the mechanism of brain function, but several neurophysiological studies have indicated that all behavior may be generated and controlled by a simple neural mechanism. Neurons basically generate electricity and secrete chemicals. The two functions together enable neurons to deal with information received from the environment and to issue appropriate commands to the glands and muscles (Klemm, 1972). With the aid of computer technology, the electroencephalogram (EEG-brain waves) has become one of the most convenient ways to monitor the overall processing reactions in the brain.

Ertl (1973) indicated that the analysis of brain waves can provide information about the learning capacity of an individual. The speed of information transfer occurring within the brain is one of the indicators of brain efficiency and hence the ability to learn. He developed a machine to measure such brain activity.

The Ertl machine (brain wave analyzer) provides neurophysiological measurements (NE, SYM, and TD scores). These measurements are obtained by having electrodes connected to the head and ear lobes of each examinee by an electrode helmet. The helmet detects and amplifies the brain waves by being placed over the left and right sensory areas of the brain. The machine does not measure intelligence as conventionally defined; rather it measures the rate of information transfer occurring within the brain in the nonalpha spectrum. Ertl (1974) reported that the machine also measures the degree of cross correlations between the EEG derived from the right and left hemispheres of the brain. Thus, Ertl (1974) proposes a more objective, culturally fair measurement and questions the use of standardized intelligence tests like the WISC as a measure of assessment. The educational application of this machine may be in its ability to measure learning potential (NE score) as well as detect early learning disabilities (TD score).

Further research on the Ertl machine is minimal at this time since the instrument is relatively new (Ertl, 1975b) and only six existed throughout the U.S.A. during this study. Data, however, by Everhart, China, and Auger (1974) indicated that an inverse relationship existed between the Wechsler Adult Intelligence Scale (WAIS) verbal scores and NE as measured by Ertl's first machine, model 0-1.

The forthcoming decade will undoubtedly observe siginificant progress to resolve the issue of empirical relationships between human intelligence and electrophysiological correlates. Perhaps this type of research may

manifest a clearer association between human brain functions and behavior.

STATEMENT OF THE PROBLEM

The primary purpose of the study was to determine relationships between the NE, Symmetry, and TD scores of the Ertl machine and WISC-Verbal (V), Performance (P), and Full scale (F) scores for a group of normal children ages 8 and 9 years (group 1) and a group of children with suspected learning disabilities of comparable ages (group 2). A secondary purpose was to determine whether significant differences existed between two groups of subjects on NE, Symmetry, and TD scores of the Ertl machine.

METHODS AND PROCEDURES

Selection of Subjects

Subjects for this study were 22 normal children (group 1) and 22 children with suspected learning disabilities (LDs) (group 2). Subjects were limited to the 8-to 10-year-old range. The two groups were similar in age, sex and race (Caucasion). The mean for normals was 8 years 9 months; the group included 13 males and nine females. The mean for group 2 was 9 years 3 months. The group included 14 males and eight females.

Procedure

Group 1 (normals) was selected by a random sampling procedure of 50 third grade children attending Brookstone, a private school in Columbus, Georgia. A letter was written and sent to the parents of the 22 children. All parents returned a slip with their approval within a week. Testing was completed during the month of May, 1975. The WISC was initially administered, followed by the Ertl machine. Subjects were not on medication (drugs) or recieving remediation for academic learning problems.

Group 2 (children with suspected learning disabilities) were selected

from two sources: (1) the Diagnostic Learning Center at Columbus College, Columbus, Georgia, and (2) the Columbus chapter of the Georgia Association for Children with Learning Disabilities. Twenty-two suspected LDs were obtained from those sources.

Permission to use Columbus College as part of group 2 was approved by the college Vice-President and two assistant directors at the center. All parents who were contacted by phone and who had children in the required age limites cooperated and signed a written statement giving permission to test. The children were all tested at the Diagnostic Learning Center, Columbus College, during the months of May-August, 1975. None of the CLDs were enrolled in special education classes at that time.

Sources of Data

Data consisted of test results from both the WISC and the Ertl machine.

The WISC was standardized on 2200 Caucasian American boys and girls selected to be representative of the 1940 U.S. census. The WISC has five verbal subtests (Information, Comprehension, Arithmetic, Similarities, and Vocabulary) and five performance subtests (Picture Completion, Picture Arrangement, Block Design, Object Assembly, and Coding). Subtests were administered according to the manual's instruction (Wechsler, 1949). Administering the WISC to each child took approximately one hour.

The Ertl machine has three separate subtests which measure various functions. These raw scores are: (a) test A, Phase score—machine emits one pulse for each milisecond that a brain wave is out of phase and displays a count of these pulses; (b) test B—average frequency of all the brain waves (alpha, beta, theta, and delta), and (c) test C—measuring alpha frequency brain rhythms exclusively. All electrophysiological measurements are taken in one complete EEG sampling over a 10-second period.

On the Ertl subtests for each child, five readings were taken. The median score was obtained for test B, with corresponding test scores for subtests A and C. Ertl (1975a) indicated that this method seemed to be most appropriate for research purposes. The digital computer on the Ertl machine then indicated the frequency of brain waves by recording the number of beats per second. The results were then adjusted by Ertl's formulas to investigate NE, Symmetry, and TD scores respectively. The NE score is composed of subtests B and C (with D as an age correction factor). Symmetry score is composed of Test A and the TD score of subtests A and B.

The total administration time per child combined with the proper placement of the electrode helmet was approximately two minutes.

Subjects were not required to answer questions or perform any tasks while on the machine, but rather were encouraged to sit comfortably (both physically and psychologically) during the administration.

The Experimental Design

Two research designs were incorporated. The first was the preexperimental, designs 1, one-shot case study (Campbell & Stanley, 1973). This design was used to investigate the correlations obtained.

The second design was quasi-experimental, non-equivalent-control group design (design 10 in Campbell & Stanley, 1973). Although a pre and post test were not formulated, groups 1 and 2 existed. This design was used to investigate regression models and differences occurring between the groups. Statistical Treatment of Data

Multiple linear regression techniques were used to analyze the data. These techniques resulted in a matrix of Pearson Product-Moment Correlation Coefficients and in a One-Way Analysis of Variance. The correlations were employed to assess the degree of relationship between the variables studied.

The "F" ratios were used to determine level of differences between groups 1 and 2. The .05 alpha level was used.

RESULTS, DISCUSSION, AND CONCLUSIONS

Correlation coefficients of the Wechsler Intelligence Scale for Children (WISC) and Ertl machine scores for the two groups are presented in Tables 1 and 2. A description of variables used for the regression models is presented in Table 3. Significant differences between Ertl machine scores for groups 1 and 2 are reported in Table 4.

To answer the question asked by Null Hypothesis One, "There will be no significant relationship between the neural efficiency (NE) scores and WISC verbal (WISC-V) scores of groups 1 and 2," the NE and WISC-V scores of group 1 were correlated. Table 1 shows that a nonsignificant r of .262 was found. As shown in Table 2, and r of -.434 was found between NE and WISC-V scores for group 2 and was significant at the .02 alpha level.

When Null Hypothesis Two, "There will be no significant relation—ship between the NE scores and WISC performance (WISC-P) of groups 1 and 2, was examined by correlating the NE and WISC-P scores of groups 1 and 2, r's of -.095 and .018 were obtained. Both correlations were nonsignificant.

The question asked by Null Hypothesis Three, "There will be no significant relationship between the Symmetry scores and WISC-V scores of groups 1 and 2", was answered by correlating the Symmetry and WISC-V scores of both groups.

An \underline{r} of -.412 was found when the Symmetry and WISC-V scores of group 1 were correlated. For group 2, an \underline{r} of .436 was found. Although \underline{r} 's for groups 1 and 2 were opposite in directions, both scores were

TABLE 1 CORRELATION MATRIX COMPUTED BETWEEN ERTL MACHINE SCORES AND WISC SCORES FOR GROUP 1 (NORMALS)

	NE		Symmetry		TD	
	r siene si	8	r	S	r	s
VIQ	.262	.12	412	.02*	.305	.08
PIQ	095	.34	4449	.01**	504	.01**
FIQ	.107	.32	118	31	.064	. 39

 $[\]underline{r}$ = Pearson correlation coefficient \underline{s} = level of significance

^{*}p .05 .01

TABLE 2

CORRELATION MATRIX COMPUTED BETWEEN ERTL MACHINE

SCORES AND WISC SCORES FOR GROUP 2 (SUSPECTED LDs)

		NE		ymmetry	TD		
	r	s	r	s	r	s	
			34				
VIQ	434	.02*	.436	.02*	305	.08	
PIQ	.018	.47	.070	.38	050	.41	
FIQ	309	.08	.369	.05*	279	.11	

r = Pearson correlation coefficient

s = level of significance

^{*}p .05

significant at .02 alpha.

Symmetry and WISC-P scores of group 1 were correlated to investigate Null Hypothesis Four, "There will be no significant relationship between the symmetry scores and WISC-P scores of groups 1 and 2". A significant \underline{r} of .449 was obtained for group 1 and a nonsignificant \underline{r} of .070 was found for group 2 (see Tables 1 and 2).

To examine Null Hypothesis Five, "There will be no significant relationship between the time difference (TD) scores and WISC-V scores of groups 1 and 2", the TD and WISC-V scores were correlated. An \underline{r} of .305 for group 1, and an \underline{r} of -.305 was obtained for group 2. Both \underline{r} 's approached significance (\underline{p} .08) as shown in Tables 1 and 2.

The testing of Null Hypothesis Six, "There will be no significant relationship between the TD scores and WISC-P scores of groups 1 and 2", resulted in an \underline{r} of -.504 for group 1, and an \underline{r} of -.050 for group 2. As shown in Tables 1 and 2 the relationship between the TD scores and the WISC-P scores for group 1 were significant at the .01 level. Those for group two were not significant.

Null Hypothesis Seven, reported in Table 4, was a comparison of the NE scores between the groups. The F ratio obtained was .1905 with $1/43 \, \underline{df}$; the probability of that being a chance occurance was .6647.

To test the differences between the symmetry scores for groups 1 and 2, Null Hypothesis Eight, as reported in Table 4, was investigated. Here, the F ratio calculated was .3607 with 1/43 df; the probability of that being a chance occurance was .5514.

When comparing the TD scores between the groups to test Null Hypothesis Nine (reported in Table 4), the F ratio computed was 4.093 with 1/43 df and P .05.

TABLE 3

A DESCRIPTION OF THE VARIABLES USED

Where the Full Model is:

 $Y_1 = a_0U + a_2x_2 + a_3x_3 + a_4x_4 + a_5x_5 + E$

The Variables are:

Y₁ = A criterion, NE score on the Ertl machine - predicted from WISC-F

 $a_0 = a_1$ through $a_5 = Partial$ regression weights

U = the Unit Vector (1 for each sample)

 x_2 = Symmetry score (SYM)

 x_3 = Time Difference score (TD)

 x_4 = Group (1, Normals)

x₅ = Group (2, Suspected LDs)

E = Error vector, difference between predicted and actual score.

TABLE 4 $\label{eq:models} \mbox{MODELS, F-RATIOS, AND } \mbox{R}^2 \mbox{ for Predicting NE SCORES }$ $\mbox{FROM WISC-F SCORES}$

					
MODELS AND EXPLANATION	R ²	df	alpha	F	P
Null Hypothesis Seven	.0045	1.43	.05	.19054	.6647
There will be no significant difference between the NE scores of groups 1 and 2.	.0000				
Full Model:					
$Y_1 = a_0 U + a_4 x_4 + a_5 x_5$					
Restriction:					
$a_4 = a_5 = a_0$					
Restricted:					
$Y_1 = a_0 U = E$					
Null Hypothesis Eight	.0085	1.43	.05	.36065	.5514
There will be no significant difference between the symmetry scores of groups 1 and 2.	.0000				
Full Model:	.0000				
$Y_2 = A_0 U + a_4 x_4 + a_5 x_5$					
Restriction:					
a ₄ = a ₅ = a ₀					
Restricted:					
$Y_2 = a_0 U + e$					
*p .05					

TABLE 4 (cont)

MODELS, F-RATIOS, AND R² FOR PREDICTING NE SCORES

FROM WISC-F SCORES

MODELS AND EXPLANATION	R^{2}	df	alpha	F	P
Null Hypothesis Nine	.0887	1.43	.05	4.0928	.0495*
There will be no signi- ficant difference between the RD scores of groups 1 and 2	.0000				
Full Model:					
$Y_3 = a_0 U + a_4 x_4 + a_5 x_5$					
Restriction:					
$a_4 = a_5 = a_0$					
Restricted:					
$Y_3 = a_0 U + E$					

^{*&}lt;u>p</u> .05

Note: See Table 3 for a description of variables used.

Although some statistically significant relationships did exist between Ertl machine scores and WISC scores, the intercorrelations were relatively low. WISC correlations with other intellectual measures generally correlated higher than results obtained with the Ertl machine scores. Results on the machine did support significant relationships opposite in sign between scores obtained on NE and WISC-V and Symmetry and WISC-V, but the variances accounted for by the correlations are inconclusive. Interestingly the two groups did differ significantly on the WISC scores for intelligence but did not differ significantly on the NE scores (learning potential) for the Ertl machine (Table 4). It appears that the low intercorrelations may be caused by greater variations on the WISC than the Ertl Machine. With regard to comparing differences between groups 1 and 2, the TD score was significant. While empirical evidence for the existence of meaningful electrophysiological correlates of human intelligence did occur in some instances, further research seems warranted utilizing children known to possess specific learning disabilities.

The results of the present study support the following conclusions:

- 1. A significant negative relationship existed between NE and WISC-V scores for group 2 and correlations between the variables for the groups were opposite in sign.
- 2. The NE score was nonsignificant when comparing differences between the groups and supported Ertl's original hypothesis (1974) that NE scores would be similar for both normals and CLDs.
- 3. Several Symmetry scores and WISC scores were significant and correlated in a positive direction for groups 1 and 2.
- 4. The relationship between Symmetry and WISC-V scores were significant and opposite in sign for both groups.

- 5. Comparison of TD scores and WISC scores revealed a significant negative relationship for group 1 between TD and WISC-P.
- 6. The difference between the TD scores for groups 1 and 2 were significant but not in the direction Ertl predicted.

It seems apparent that additional research needs to be conducted regarding the relationships between scores obtained on the Ertl machine and human intelligence as measured by the WISC. Perhaps the present design could be replicated with these changes: 1) An increased sample size; 2) The experimental group could be diagnosed learning disabled children, rather than suspected LDS; and 3) The sample studied could include more children from lower socioeconomic levels, including minority group students.

It must be remembered that generalizations from the present research are limited because of the lack of reliability and validity data on the Ertl machine. Moreover, though this work identified some correlations between the Ertl machine and WISC, the WISC is a highly language oriented instrument. Future studies should be conducted with the Ertl machine and other measures of intelligence. Finally, WISC subtests, in addition to WISC scale scores, should be carefully examined in relationship to Ertl machine socres.

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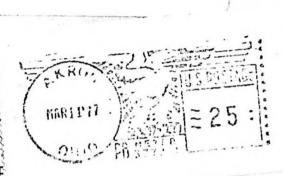


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